

## Bioconvective variable viscosity flow of Carreau nanofluid with external heat source and nonlinear radiation: Analysis with convective heat and mass constraints



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## ABSTRACT

In this study, an unsteady model for Carreau nanofluid with microorganism decomposition is developed. The viscosity and thermal conductivity of the Carreau nanofluid are considered variable. Magnetic and porosity effects are included using a magneto-porosity parameter. An additional heat source is introduced to improve heat transfer. Nonlinear analysis is applied for radiative applications. The flow is modeled using an oscillatory stretching surface. Convective mass and heat constraints are used to analyze the problem. Analytical computations are performed on the developed model. The significance of various parameters for the thermal problem is discussed. The results may enhance the performance of transport problems, heat transmission, energy systems, and thermal devices.

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## 1. Introduction

Driven by advances in nanotechnology, researchers have argued for the integration of nanoscale solid particles into heating and cooling mechanisms as a new energy source. Thanks to their superior thermal efficiency, these nanomaterials are recognized as an optimal thermal energy source. The impact of nanomaterials on thermal performance has made significant contributions in various sectors, including industrial manufacturing, heating appliances, nuclear power, chemical engineering, healthcare, and automobile engines. A review of the literature reveals various studies that highlight the benefits of nanofluids, enhanced by additional thermal sources and innovative designs. Javaid et al. (2022) presented the Burgers nanofluid analysis in the annulus region. Hosseinzadeh et al. (2023) described the role of nanofluid in enhancing the impact of the heat transfer phenomenon. Sheikholeslami et al. (2023) utilized solar applications based on the nanofluid flow within a porous sink surface. Shamshuddin et al. (2023) described the sensor plate flow subject to nanofluid interaction. Jalili et al. (2023) examined the Hall

outcomes for nanofluid in an analytical way. The power law nanofluid with gold metallic particles was analyzed with optimized impact in the investigation of Sharma et al. (2023a). Gangadhar et al. (2024) evaluated the squeezing analysis for nanofluid in radiated surfaces. Mebarek-Oudina and Chabani (2023) analyzed the thermal energy performances utilized by nanoparticles with PCM applications. Rafique et al. (2023) discussed the slip role in fluctuated viscosity nanofluid flow containing hybrid particles. Dharmiah et al. (2023) analyzed the nanofluid with Howarth's wavy path along with activation energy. Sharma et al. (2023b) described the micropolar nanofluid analysis for Bayesian flow. Eid et al. (2023) inspected the Dufour analysis against the uniformly driven flow of nanofluid on an inclined surface. Bhatti et al. (2023) examined the Darcy-Forchheimer aspect due to nanofluid-driven flow analytically. Khan and Shehzad (2020) utilized the Carreau nanofluid with variable thermal conductivity assessment due to moving periodic surfaces.

The phenomenon of bioconvection refers to the coordinated movement of microorganisms in a fluid triggered by a variety of environmental factors. This process involves the complex interaction of nanofluids with gyrotactic microorganisms, which underlies the functionality of the bioconvection framework. Bioconvection has diverse applications in the fields of biotechnology and environmental sciences. It allows the suspension of bacteria and other microorganisms within nanoparticles, facilitating their use in biofuel development,

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environmental monitoring, and fertilizers, among other applications. Additionally, bioconvection holds significant importance in chemical engineering and biotechnology, introducing innovative approaches to these disciplines. Mabood et al. (2023) predicted the bioconvective enrollment for nanofluid with impressive heat transfer performances. Li et al. (2023a) utilized the pattern for bioconvection due to the melting heat nanofluid problem. Khan et al. (2023) discussed the analysis of microorganisms suspended in nanofluid under an optimized pattern. Patil et al. (2023) described the wedge flow of nanofluid with bioconvective judgment. Ghachem et al. (2023) analyzed the numerical treatment for the bioconvective-supported nanofluid problem. A study performed by Jabeen et al. (2024) explained the microorganism's role in the stability of nanofluid. Haq et al. (2023) evaluated the rotating flow with bioconvective analysis endorsed by Sutterby nanofluid. Hussain et al. (2023) predicted the 3D analysis for bioconvective nanofluid in Williamson fluid. Li et al. (2023b) directed the entropy phenomenon for Carreau nanofluid in the presence of bioconvection impact. The lubricated surface bioconvective analysis for nanofluid was utilized by Maatoug et al. (2023). Anjum et al. (2023) expressed the cross-nanofluid transport with gyrotactic microorganisms and activation energy. Ahmed et al. (2023) described the bioconvective investigation while treating the thermal properties of nanofluid. The Keller Box simulations for nanofluid with gyrotactic microorganisms were claimed by Abbas et al. (2023).

This investigation deals with the assessment of bioconvective patterns for Carreau nanofluid with variable viscosity. The combined features of magnetic force and porous medium have been entertained. The assumptions for heat transfer are directed by variable thermal conductivity. Nonlinear radiated impact and external heat transfer effects are accounted. The problem is subject to convective mass and thermal constraints. After developing the model, the simulations are performed using the homotopy analysis method (HAM). The physical dynamic of the problem is addressed.

## 2. Statement of problem

An incompressible Carreau nanofluid flow under the decomposition of microorganisms has been investigated. The periodically accelerating porous surface accounting the flow. The microorganisms' suspensions are utilized. The role of variable thermal conductivity and viscosity is taken into account. The additional outcomes for heat transfer are regarded by heat source. The impact of nonlinear radiation is taken into account. The magnetic force acts along normal directions. The 2D flow problem is established in the coordinate system with horizontal velocity  $u$  and normal velocity  $v$ . Such constraints lead to the following set of equations (Khan and Shehzad, 2020; Mabood et al., 2023):

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0, \tag{1}$$

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = \frac{1}{\rho_f} \frac{\partial}{\partial y} \left( \mu_f(T) \frac{\partial u}{\partial y} \right) + \nu_f \frac{3(n-1)}{2} \lambda_*^2 \frac{\partial^2 u}{\partial y^2} \left( \frac{\partial u}{\partial y} \right)^2 - \frac{\sigma B_0^2}{\rho_f} u - \frac{\nu \phi_0}{k^*} u, \tag{2}$$

$$\frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \frac{1}{\rho c_p} \frac{\partial}{\partial y} \left( k(T) \frac{\partial T}{\partial y} \right) + \frac{16\sigma^*}{3k^*(\rho c_p)_f} \frac{\partial}{\partial y} \left\{ T^3 \frac{\partial T}{\partial y} \right\} + \frac{q^*}{(\rho c_p)_f} (T_f - T_\infty) + Y_e \left\{ \text{and } D_B \frac{\partial T}{\partial y} \frac{\partial C}{\partial y} \right\}, \tag{3}$$

$$\frac{\partial C}{\partial t} + u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} = D_B \frac{\partial^2 C}{\partial y^2} + \frac{D_T}{T_\infty} \frac{\partial^2 T}{\partial y^2} - k_c (C_f - C_\infty), \tag{4}$$

$$\frac{\partial n}{\partial t} + u \frac{\partial n}{\partial x} + v \frac{\partial n}{\partial y} + \frac{b_l w_l}{(C_w - C_\infty)} \left[ \frac{\partial}{\partial y} \left( n \frac{\partial C}{\partial y} \right) \right] = D_m \left( \frac{\partial^2 n}{\partial y^2} \right). \tag{5}$$

Important physical quantities are time-constant  $\lambda_*$ , fluid density  $\rho_f$ , electrical conductivity  $\sigma$ , time  $t$ , external heat source coefficient  $q^*$ , porous medium  $\phi$ , permeability medium  $k^*$ , temperature  $T$ , variable thermal conductivity  $k(T)$ , Stefan Boltzmann  $\sigma$ , Rosseland mean absorption  $k^*$ , Brownian diffusion  $D_B$ , thermo-diffusion  $D_T$ , ambient temperature  $T_\infty$ , free stream concentration  $C_\infty$ , effective heat transfer ratio between particles to fluid  $Y_e$ , reaction rate  $\kappa$ , chemotaxis constant  $b_l$  and swimming cells' speed  $w_l$ . The following assumptions are used for variable viscosity; the Reynolds exponential theory is used as:

$$\mu_f(\theta) = e^{-(A\theta)} = 1 - (A\theta) + O(A^2), \tag{6}$$

with  $A$  (viscosity coefficient).

The following assumptions are used for variable thermal conductivity:

$$k(T) = k_\infty \left[ 1 + \delta \frac{(T_f - T_\infty)}{\Delta T} \right], \tag{7}$$

where, ambient conductivity is defined by  $k_\infty$  while  $\delta$  explain the variable thermal conductivity coefficient.

The problem is incorporated with the following boundary constraints (Khan and Shehzad, 2020; Mabood et al., 2023):

$$\left. \begin{aligned} u = u_\omega = bx \sin \lambda t, \quad v = 0, \quad -k \frac{\partial T}{\partial y} = h_1 (T_f - T) \\ -D_B \frac{\partial C}{\partial y} = h_2 (C_f - C), \quad n = n_w \quad \text{at } y = 0, \quad t > 0 \end{aligned} \right\} \tag{8}$$

$$u \rightarrow 0, \quad T \rightarrow T_\infty, \quad C \rightarrow C_\infty, \quad n \rightarrow n_\infty \quad \text{at } y \rightarrow \infty \tag{9}$$

where,  $\lambda$  defining the accelerating frequency,  $h_1$  be heat transfer coefficient and  $h_2$  represent the mass transfer coefficient.

The problem is entertained in view of the following variables (Khan and Shehzad, 2020):

$$\xi = \sqrt{\frac{b}{\nu}} y, \quad \tau = t \Omega_s, \quad u = b x f_y(\xi, \tau), \quad v = -\sqrt{\nu b} f(\xi, \tau), \tag{10}$$

$$\theta(\xi, \tau) = \frac{T - T_\infty}{T_f - T_\infty}, \quad \phi(\xi, \tau) = \frac{C - C_\infty}{C_f - C_\infty}, \quad \chi(\xi, \tau) = \frac{n - n_\infty}{n_w - n_\infty}.$$

The new arranged system is:

$$\begin{aligned} (1 - A\theta) f_{\xi\xi\xi} - S f_{\xi\tau} - f_\xi^2 + f f_{\xi\xi} + \frac{3(n-1)We}{2} f_{\xi\xi} f_{\xi\xi}^2 - \\ H a f_\xi = 0, \end{aligned} \tag{11}$$

$$\frac{1}{Pr} [1 + \epsilon\theta + \frac{4}{3} Rd\{1 + (\theta_f - 1)\theta\}^3] \theta_{\xi\xi} + \frac{1}{Pr} [\epsilon + 4Rd(\theta_f - 1)(1 + (\theta_f - 1)\theta)^2] (\theta_{\xi})^2 + f\phi_{\xi} + Nb\theta_{\xi}\phi_{\xi} + Nt(\theta_{\xi})^2 - S\theta_{\tau} + Q\theta = 0 \tag{12}$$

$$\varphi_{\xi\xi} + \frac{Nt}{Nb}\theta_{\xi\xi} - S(Sc)\varphi_{\tau} + Scf\varphi_{\xi} - (Sc)kr\varphi = 0, \tag{13}$$

$$\chi_{\xi\xi} - S(Lb)\chi_{\tau} + Lb\chi_{\xi} - Pe[\varphi_{\eta\eta}(\chi + \Lambda_g) + \chi_{\xi}\varphi_{\eta}] = 0. \tag{14}$$

Subjecting to dimensionless constraints:

$$f_{\xi}(0, \tau) = \sin \tau, f(0, \tau) = 0, \theta_{\xi}(0, \tau) = -\gamma_1[1 - \theta(0, \tau)], \phi_{\xi}(0, \tau) = -\gamma_2[1 - \phi(0, \tau)], \chi(0, \tau) = 1, \tag{15}$$

$$f_{\xi}(\infty, \tau) \rightarrow 0, \theta(\infty, \tau) \rightarrow 0, \varphi(\infty, \tau) \rightarrow 0, \chi(\infty, \tau) \rightarrow 0 \tag{16}$$

where,  $We$  is the Carreau fluid parameter, the magneto-porosity parameter,  $\beta$  is the magneto-porosity constant,  $\theta_f$  is surface heating constant,  $\gamma_2$  the concentration Biot number,  $S$  is oscillation frequency to stretched rate ratio,  $Q_f$  is the heat generation/absorption coefficient,  $Rd$  is the radiation parameter,  $Nb$  is the Brownian parameter,  $Pe$  is the Peclet number,  $Nt$  is the thermophoresis constant,  $\Lambda_g$  represents the microorganisms' concentration fluctuation,  $\gamma_1$  is the thermal Biot number and  $Lb$  bioconvection Lewis number having the following relations:

$$We = \lambda_*^2 b^2 x^2 / \nu_f, \quad \beta = \frac{\sigma B_0^2}{b\rho_f} + \frac{\nu\varphi}{bk}, \quad S = \Omega_s/b, \quad Rd = 4\sigma^* T_{\infty}^3 / 3k^* k_{\infty}, \quad \theta_f = T_f/T_{\infty}, \quad Nb = Y_e D_B (C_f - C_{\infty}) / \nu_f, \quad Nt = Y_e D_T (T_f - T_{\infty}) / T_{\infty} \nu_f, \quad Q_f = q^* / b(\rho c_p)_f, \quad \Lambda_g = n_{\infty} / (n_w - n_{\infty}), \quad Pe = b_l w_l / D_m, \quad Lb = \nu_f / D_m, \gamma_1 = (h_1/k) \sqrt{\nu_f/b}, \gamma_2 = (h_2/D_m) \sqrt{\nu_f/b}.$$

Defining the local Nusselt number, local Sherwood number, and motile density number (Shamshuddin et al., 2023; Mabood et al., 2023):

$$\frac{Nu}{\sqrt{Re_x}} = -\left(1 + \frac{4}{3} Rd\theta_w^3(0, \tau)\right) \frac{Su}{\sqrt{Re_x}} = -\varphi_{\xi}(0, \tau), \frac{Nn}{\sqrt{Re_x}} = -\chi_{\xi}(0, \tau). \tag{17}$$

### 3. Analytical scheme

The main problem involves complex partial differential equations (PDEs), making it challenging to compute a solution. The solution is developed using the HAM, which is preferred due to its high accuracy. To begin the simulations, we first select an initial guess:

$$f_0(\xi, \tau) = \sin \tau (1 - e^{-\xi}), \theta_0(\xi) = e^{-\xi}, \varphi_0(\xi) = e^{-\xi}, \chi_0(\xi) = e^{-\xi}. \tag{18}$$

With auxiliary linear operators

$$\mathcal{E}_f = \frac{\partial^3}{\partial \xi^3} - \frac{\partial}{\partial \xi}, \mathcal{E}_{\theta} = \frac{\partial^2}{\partial \xi^2} - 1, \mathcal{E}_{\varphi} = \frac{\partial^2}{\partial \xi^2} - 1, \mathcal{E}_{\chi} = \frac{\partial^2}{\partial \xi^2} - 1 \tag{20}$$

with solution:

$$\mathcal{E}_f \left( \sum_{r=0}^2 \omega_{r+1} e^{(r-1)\xi} \right) = 0, \tag{21}$$

$$\mathcal{E}_{\theta} \left( \sum_{r=3}^4 \omega_{r+1} e^{(-1)^r \xi} \right) = 0, \tag{22}$$

$$\mathcal{E}_{\chi} \left( \sum_{r=5}^6 \omega_{r+1} e^{(-1)^r \xi} \right) = 0, \tag{23}$$

$$\mathcal{E}_{\phi} \left( \sum_{r=7}^8 \omega_{r+1} e^{(-1)^r \xi} \right) = 0, \tag{23}$$

where,  $\Psi_j (j = 1, 2, \dots, 9)$  are unknown constants.

### 4. Convergence analysis

The desirable accuracy obtained via HAM is based on values of auxiliary coefficients. These auxiliary coefficients  $h_f, h_{\theta}, h_{\phi}$  and  $h_{\chi}$  play a vital role in ensuring the convergence region. The illustration of these parameters is achieved by plotting  $h$ -curve in Fig. 1. For an admissible range of parameters, the numerical values can be chosen from  $-1.6 \leq h_f \leq -0.1$ ,  $-1.9 \leq h_{\theta} \leq 0.1$ ,  $-1.7 \leq h_{\phi} \leq -0.2$  and  $-1.8 \leq h_{\chi} \leq 0$ .

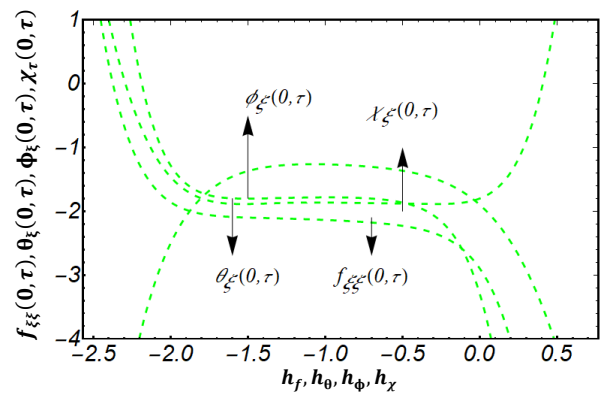


Fig. 1:  $h$ -curves for  $f_{\xi\xi}, \theta_{\xi}, \varphi_{\xi}$  and  $\chi_{\xi}$

### 5. Numerical model verification

Before analyzing the physical aspects of the problem, the computed results are verified first. Table 1 presents the accuracy of simulated results compared to the findings of Abbas et al. (2008) and Zheng et al. (2023) with the variation of  $\tau$ . A good concordance between the results is noticed.

Table 1: Comparison of  $f_{\xi\xi}(0, \tau)$  with Abbas et al. (2008) and Zheng et al. (2023) when  $A = 0, S = n = 1, M = 12$

$\tau$	Abbas et al. (2008)	Zheng et al. (2023)	Present results
$1.5\pi$	11.678656	11.678656	11.678656
$5.5\pi$	11.678707	11.678706	11.678706
$9.5\pi$	11.678656	11.678656	11.678656

### 6. Results and discussion

Fig. 2a presents the change of velocity  $f_{\xi}$  with time  $\tau$  for various Carreau fluid coefficients  $We$ . An increasing amplifying of velocity with oscillatory behavior is observed. The oscillatory nature of  $f_{\xi}$  is exhibited due to the sinusoidal motion of velocity. The Weissenberg number is a dimensionless number that describes the ratio of elastic to viscous forces in a fluid flow. It is often used in the study of non-Newtonian fluids, where the fluid's viscosity can change with the flow conditions. In Fig. 2a, as  $We$  increases, the amplitude of the oscillations seems to decrease slightly, and the waveform appears to become less sinusoidal and more complex. This

implies that higher elastic effects (higher  $We$ ) dampen the oscillatory behavior of  $f_\xi$ .

Fig. 2b identifies the outcomes of magneto-porosity parameter  $\beta$  on judgement of  $f_\xi$ . A reducing oscillation is preserved for  $f_\xi$  in view of larger  $\beta$ . Basically,  $\beta$  summarizing the joint role of magnetic force and porous media. For higher values of  $\beta$ , the peaks and troughs of the waveform are slightly more pronounced, suggesting that  $\beta$  amplifies the

characteristics of the oscillations. The magnetic force contributes to the Lorentz force, while the effects of porous media are explained by the permeability of the porous region. Both forces significantly reduce the velocity. Fig. 2c comprises the assessment for  $f_\xi$  in view of variable viscosity coefficient  $A$ . Slower velocity with declining amplitude is exhibited for an increase in  $A$ .

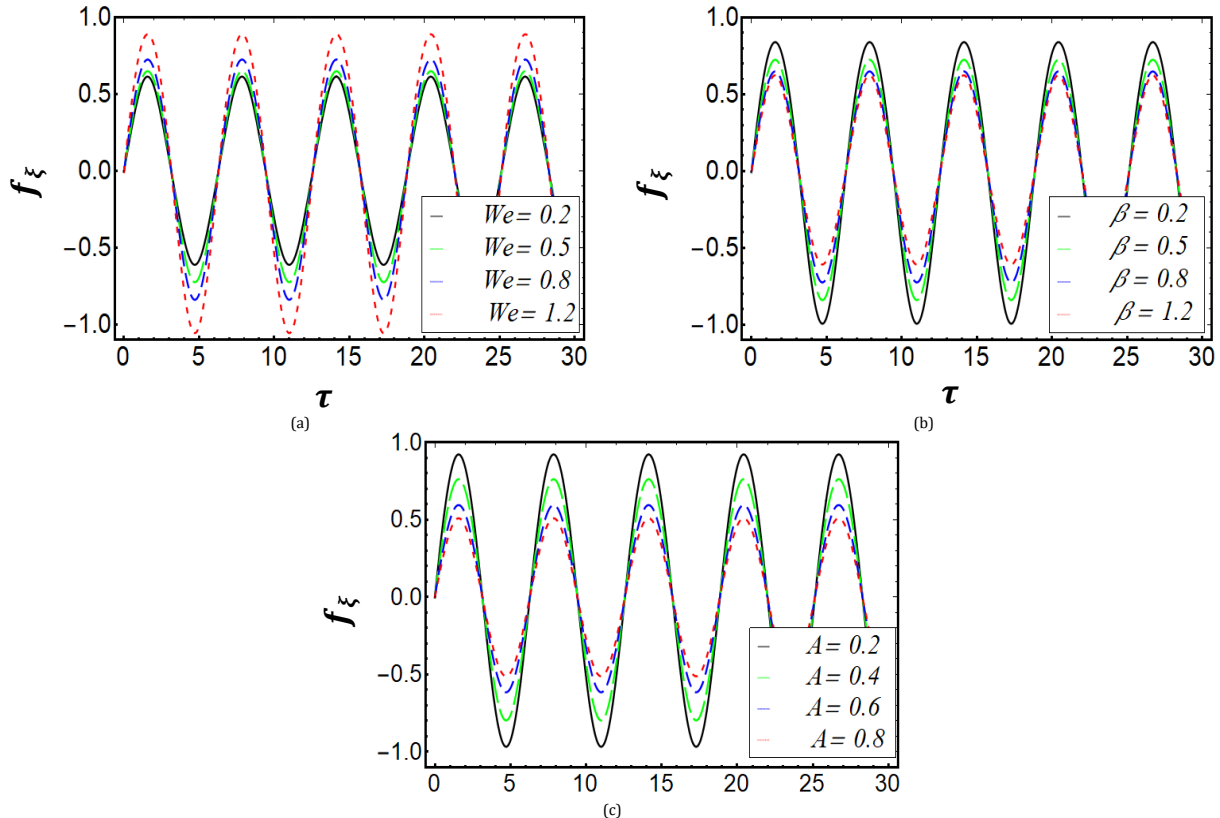


Fig. 2: Effects of (a)  $We$  (b)  $\beta$  (c)  $A$  on the temporal variation of  $f_\xi$

Fig. 3a illustrates an analysis of the temperature profile  $\theta$  due to larger variable viscosity parameter  $A$ . shows an increase in the temperature profile  $\theta$  as  $A$  increases. This is due to the temperature-dependent viscosity, and as viscosity changes, it affects the thermal energy distribution. The onset of the Carreau fluid coefficient  $We$  on temperature field  $\theta$  has been evaluated in Fig. 3b. The decrement is noted in the evaluation of  $\theta$  due to  $We$ . The decrement in  $\theta$  with increasing  $We$  suggests that elastic forces in the fluid act to decrease the temperature profile, which is due to a change in the internal fluid motion that reduces thermal energy distribution. Fig. 3c justifies the determined role of magneto-porosity parameter  $\beta$  on  $\theta$ . The enhanced truncation in  $\theta$  with justified range of  $\beta$  has been exhibited. Physically,  $\beta$  attributes both magnetic force and porous medium applications which enhance the thermal phenomenon. The observed truncation in  $\theta$  with an increase in  $\beta$  indicates that magnetic forces and the porosity of the medium affect the convection and conduction processes by altering the flow paths and enhancing thermal dissipation. Fig. 3d contributes the role of variable

thermal conductivity constant  $\delta$  on  $\theta$ . The variable assumptions for thermal conductivity leading to improvement in  $\theta$ . In different energy systems, the thermal conductivity of involved materials cannot be treated as a constant. The interpretation that variable thermal conductivity leads to an improvement in  $\theta$  aligns with the concept that a material's ability to conduct heat can vary with temperature, and accounting for this variability can lead to a more accurate description of the thermal profile.

Fig. 4a claims the truncation in temperature field  $\theta$  by contributing the effective role of surface heating parameter  $\theta_f$ . The association of  $\theta_f$  is associated to nonlinear radiated phenomenon. With increasing  $\theta_f$ , temperature get enlarging. The investigation performed in Fig. 4b aims to involve the effects of external heat source parameter  $Q_f$  on  $\theta$ . The contribution of  $Q_f$  present external heat source to moving surface, which enhances the rate of temperature within fluid particles. Fig. 4c analyzes the significance of thermal Biot number  $h_1$  on  $\theta$ . A raise in  $\theta$  subject to  $h_1$  is noticed. Physically,  $h_1$  accounting the effective features of the heat transfer

coefficient due to which  $\theta$  get boosted. Fig. 4d shows an increasing enrollment in pattern of  $\theta$  due to

thermophoresis parameter  $Nt$ . Such outcomes are due to thermos-diffusion phenomenon.

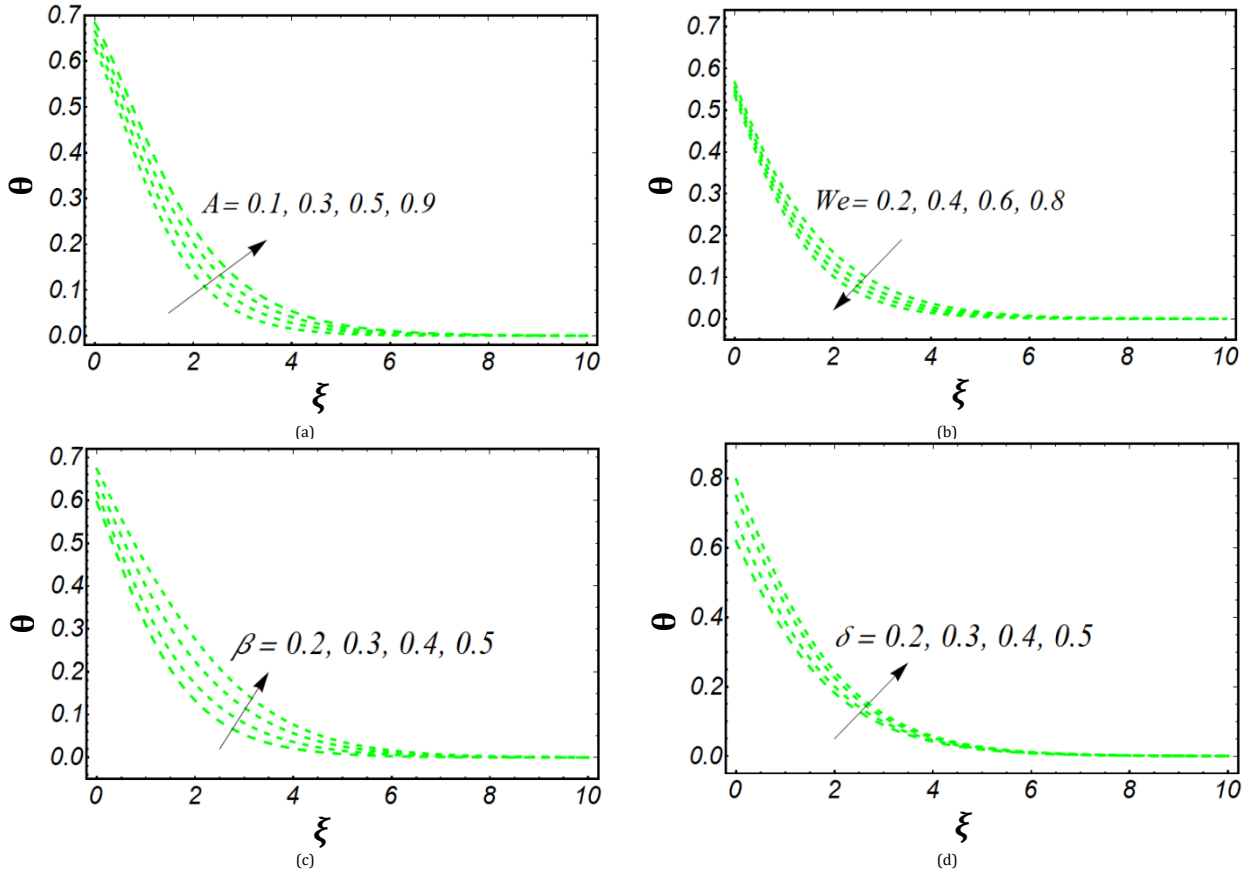


Fig. 3: Effects of (a)  $A$  (b)  $We$  (c)  $\beta$  (d)  $\delta$  on the temperature profile

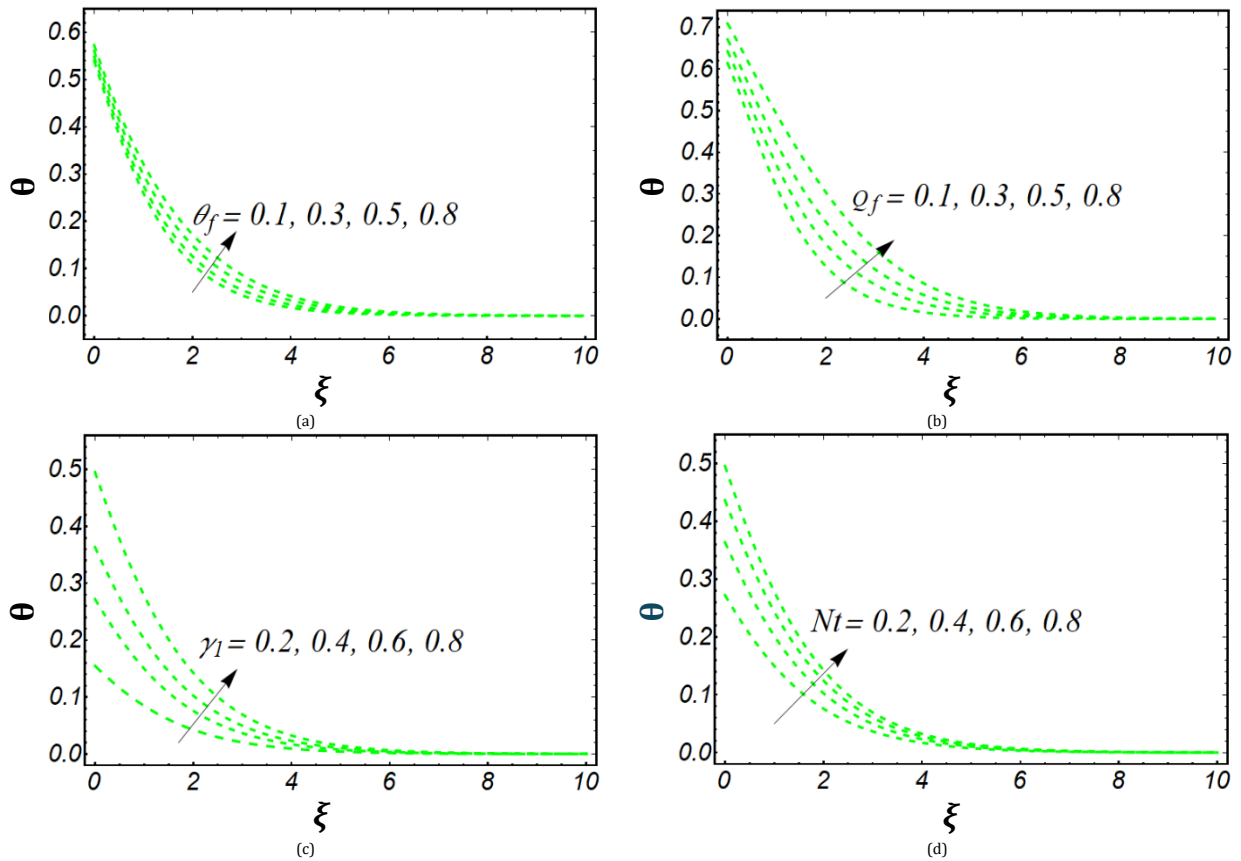


Fig. 4: Effects of (a)  $\theta_f$  (b)  $Q_f$  (c)  $\gamma_1$  (d)  $Nt$  on the temperature profile

Fig. 5a discusses the truncated profile of concentration  $\phi$  due to concentration Biot number  $\gamma_2$ . Upshot observations are evaluated in the assessment of  $\phi$  due to  $\gamma_2$ . Due larger  $\gamma_2$ , the mass transfer coefficient enhances. Fig. 5b determines the outcomes for Schmidt number  $Sc$  on  $\phi$ . Declining effects of  $Sc$  are noticed on  $\phi$ . Such decreasing outcomes due to low mass diffusivity. Fig. 5c

addresses the analysis for  $\phi$  by varying variable viscosity coefficient  $A$ . Enhancement is predicted for  $\phi$  against  $A$ . Fig. 5d presents the analysis for  $We$  on  $\phi$ . Lower changes in  $\phi$  due to  $We$  are claimed. Fig. 5e announces the concentration of nanofluid decomposition decreases when the chemical reaction parameter gets  $kr$  varied.

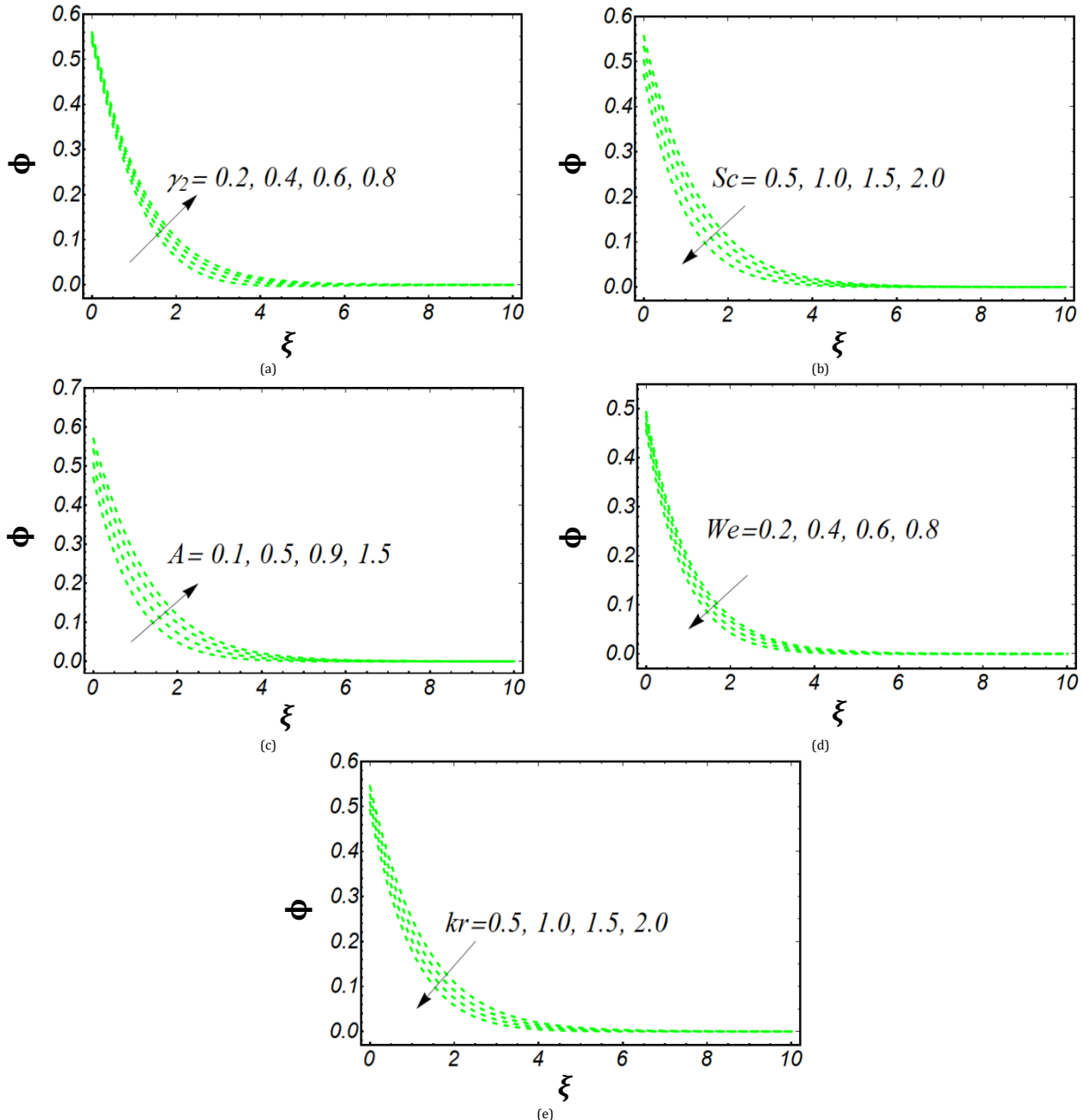


Fig. 5: Effect of (a)  $\gamma_2$  (b)  $Sc$  (c)  $A$  (d)  $We$  (e)  $kr$  on the concentration profile

Fig. 6a reports that interaction for microorganisms' profile  $\chi$  subject to  $We$ . The microorganisms profile showing reducing prediction due to  $We$ . Fig. 6b addresses the continuation of Peclet number  $Pe$  on  $\chi$ . Reducing change in  $\chi$  is exhibited for variation of  $Pe$ . Less motile diffusivity is involved for enlarging  $Pe$  which turn down the assessment of  $\chi$ . Same observations are exhibited for bioconvective Lewis number in Fig. 6c. Table 2 presents the numerical impact of different

parameters on  $-\theta_\xi(0, \tau)$ ,  $-\phi_\xi(0, \tau)$  and  $-\chi_\xi(0, \tau)$ . An increase in  $We$  leads to a steeper negative gradient, which suggests that elastic effects are enhancing heat transfer. Similar to  $\theta$ ,  $\phi$  also shows a more negative gradient with increasing  $We$ , indicating a stronger rate of decrease in concentration due to the enhanced mixing. As with  $\theta$  and  $\phi$ , a larger  $We$  results in a larger negative gradient for microorganism concentration, implying that elasticity is dispersing the microorganisms more

effectively. The temperature gradient decreases as  $\beta$  increases, which indicates that magnetic forces and porosity impede the transfer of heat, by altering flow patterns. The gradient of  $\phi$  also decreases with  $\beta$ , suggesting that the diffusion and advection of the chemical species is being moderated.

The microorganism concentration gradient shows a decrease with higher  $\beta$ , due to the magnetic field's alignment effects or the porous medium's filtration effects. A varying  $S$  affects the temperature gradient, suggesting that unsteady flow is impacting

thermal transfer rates. Changes in  $S$  affect  $\phi$ 's gradient, which implies that unsteady flow affects the dispersion of nanoparticles. The gradient of  $\chi$  changes with  $S$ , indicating that flow unsteadiness effectively disperses the microorganisms. Higher  $A$  values show a more negative temperature gradient, suggesting that variable viscosity enhances the heat transfer. A similar trend is observed for  $\phi$ , indicating that the concentration of the nanoparticles decreases more rapidly with variable viscosity.

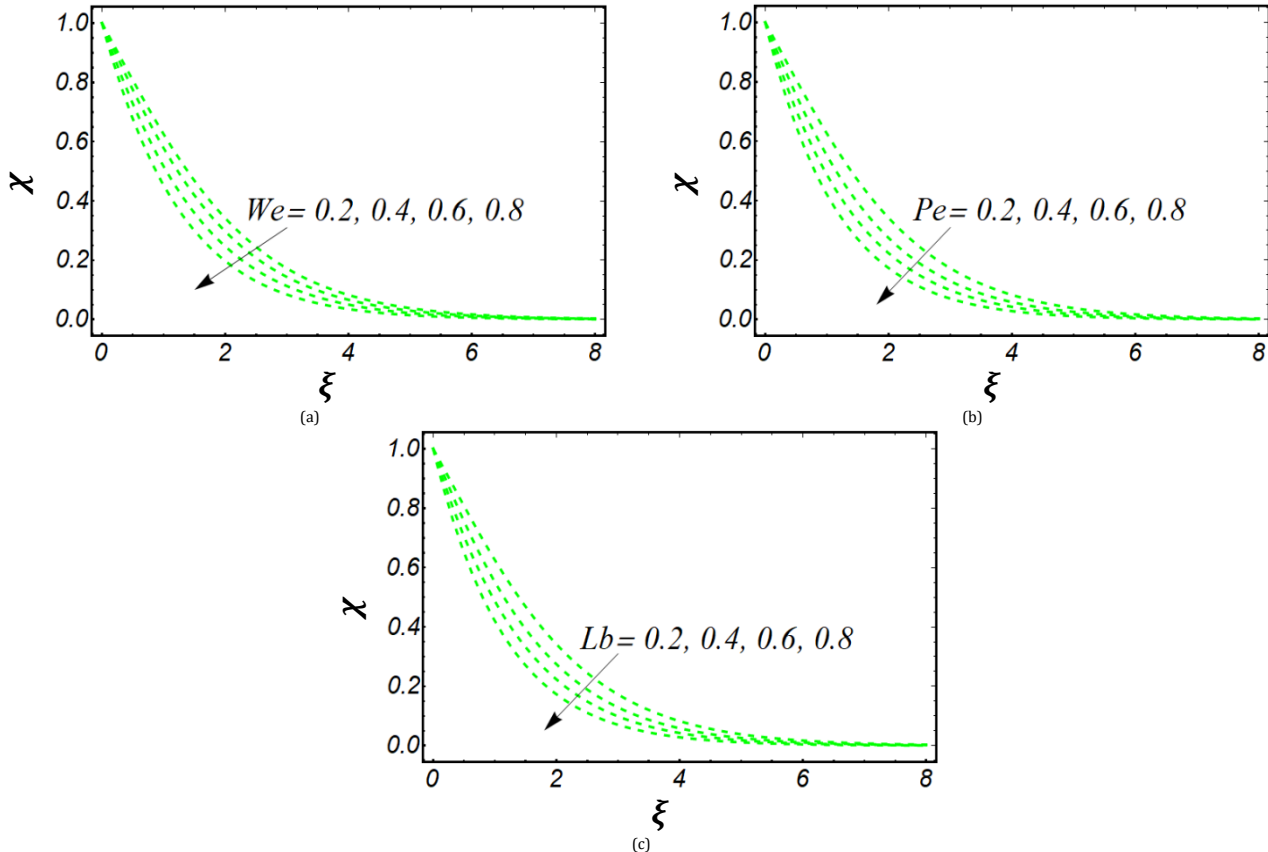


Fig. 6: Effects of (a)  $We$  (b)  $Pe$  (c)  $Lb$  on the microorganism's profile

Table 2: Numerical impact of the governing parameters on  $-\theta_\xi(0, \tau)$ ,  $-\phi_\xi(0, \tau)$  and  $-\chi_\xi(0, \tau)$

$We$	$\beta$	$S$	$Pr$	$Nb$	$A$	$\delta$	$-\theta_\xi(0, \tau)$	$-\phi_\xi(0, \tau)$	$-\chi_\xi(0, \tau)$
0.2	0.1	0.5	0.3	0.3	0.7	0.5	0.84357	0.66365	0.54320
0.4							0.86851	0.69748	0.57784
0.8							0.91478	0.73012	0.61297
0.3	0.4						0.81254	0.67789	0.57754
	0.6						0.76021	0.64320	0.54751
	1.0						0.73785	0.62785	0.51325
		0.2					0.76965	0.64624	0.59781
		0.4					0.72789	0.62389	0.51329
		0.8					0.68365	0.58145	0.47625
			0.4				0.79785	0.65751	0.54751
			1.0				0.83778	0.67017	0.58325
			1.4				0.87325	0.71754	0.63145
				0.2			0.75785	0.64632	0.52320
				0.4			0.74445	0.61145	0.47965
				0.6			0.71896	0.57785	0.45857
					0.4		0.74325	0.67554	0.56021
					0.8		0.72034	0.64789	0.53324
					1.2		0.67780	0.58215	0.51785
						0.4	0.79447	0.62785	0.54715
						1.0	0.83320	0.66532	0.57750
						1.6	0.84497	0.69785	0.59302

The trend is consistent for microorganism concentration as well, with variable viscosity potentially causing a more rapid decrease in

concentration. The gradient of temperature seems to be affected by  $\delta$ , indicating that the temperature profile is sensitive to changes in thermal

conductivity. The gradient of  $\phi$  shows variability with  $\delta$ , suggesting an interaction between thermal properties and chemical dispersion. The microorganism concentration gradient also changes with  $\delta$ , which means that thermal conductivity indirectly affects microorganism distribution.

## 7. Conclusions

In this study, a dynamic model is presented for the Carreau nanofluid that incorporates the decomposition of microorganisms. The viscosity and thermal conductivity of the Carreau nanofluid are considered to vary. The effects of magnetism and porosity are integrated via the magneto-porosity parameter. Additionally, the introduction of extra heat sources aims to improve the heat transfer issue. A nonlinear approach is adopted for applications involving radiation. An oscillating stretching surface facilitates the promotion of flow. The examination of the issue employs convective mass and heat restrictions. Analytical methods are applied to tackle the formulated problem. The main results can be summarized as follows:

- The velocity profile of the nanofluid is enhanced when larger numerical values are assigned to the Carreau fluid parameter.
- A minimal numerical impact on the velocity profile is observed with the viscosity parameter.
- Heat transfer is significantly increased by the magneto-porosity parameter and the surface heating parameter.
- The addition of an extra heat source effectively boosts the temperature profile.
- As the thermal Biot number increases, so does the temperature profile.
- The concentration profile decreases with the Carreau fluid parameter and the chemical reaction constant.
- An improving trend in the concentration profile is observed with the concentration Biot number.
- Both the Nusselt number and the Sherwood number are reduced by the magneto-porosity parameter.

## Compliance with ethical standards

## Conflict of interest

The author(s) declared no potential conflicts of interest with respect to the research, authorship, and/or publication of this article.

## References

- Abbas T, Al-Khaled K, Raza AH, Ayadi M, Chammam W, and Khan SU (2023). Inclined magnetized flow of radioactive nanoparticles with exponential heat source and slip effects: Keller box simulations. *Journal of Nanofluids*, 12(2): 571-579. <https://doi.org/10.1166/jon.2023.1935>
- Abbas Z, Wang Y, Hayat T, and Oberlack M (2008). Hydromagnetic flow in a viscoelastic fluid due to the oscillatory stretching surface. *International Journal of Non-Linear Mechanics*, 43(8): 783-793. <https://doi.org/10.1016/j.ijnonlinmec.2008.04.009>
- Ahmed J, Nazir F, Fadhl BM, Makhdoum BM, Mahmoud Z, Mohamed A, and Khan I (2023). Magneto-bioconvection flow of Casson nanofluid configured by a rotating disk in the presence of gyrotactic microorganisms and Joule heating. *Heliyon*, 9(8): e18028. <https://doi.org/10.1016/j.heliyon.2023.e18028> PMID:37664738 PMCID:PMC10469572
- Anjum N, Khan WA, Azam M, Ali M, Waqas M, and Hussain I (2023). Significance of bioconvection analysis for thermally stratified 3D Cross nanofluid flow with gyrotactic microorganisms and activation energy aspects. *Thermal Science and Engineering Progress*, 38: 101596. <https://doi.org/10.1016/j.tsep.2022.101596>
- Bhatti MM, Al-Khaled K, Khan SU, Chammam W, and Awais M (2023). Darcy-Forchheimer higher-order slip flow of Eyring-Powell nanofluid with nonlinear thermal radiation and bioconvection phenomenon. *Journal of Dispersion Science and Technology*, 44(2): 225-235. <https://doi.org/10.1080/01932691.2021.1942035>
- Dharmaiah G, Dinarvand S, Prasad JR, Noeiaghdam S, and Abdollahzadeh M (2023). Non-homogeneous two-component Buongiorno model for nanofluid flow toward Howarth's wavy cylinder with activation energy. *Results in Engineering*, 17: 100879. <https://doi.org/10.1016/j.rineng.2023.100879>
- Eid MR, Jamshed W, Goud BS, Ibrahim RW, El Din SM, Abd-Elmonem A, and Abdalla NSE (2023). Mathematical analysis for energy transfer of micropolar magnetic viscous nanofluid flow on permeable inclined surface and Dufour impact. *Case Studies in Thermal Engineering*, 49: 103296. <https://doi.org/10.1016/j.csite.2023.103296>
- Gangadhar K, Victoria EM, and Chamkha AJ (2024). Effect of entropy minimization and melting heat on gold-magnesium oxide hybrid nanofluid in squeezing channel with magnetic field with radiation. *International Journal of Modern Physics B*, 38(14): 2450172. <https://doi.org/10.1142/S0217979224501728>
- Ghachem K, Ahmad B, Noor S, Abbas T, Khan SU, Anjum S, Alwadai N, and Kolsi L (2023). Numerical simulations for radiated bioconvection flow of nanoparticles with viscous dissipation and exponential heat source. *Journal of the Indian Chemical Society*, 100(1): 100828. <https://doi.org/10.1016/j.jics.2022.100828>
- Haq F, Rahman MU, Khan MI, Abdullaeva BS, and Altuijri R (2023). Mathematical modeling and theoretical analysis of bioconvective magnetized sutterby nanofluid flow over rotating disk with activation energy. *BioNanoScience*, 13(4): 1849-1862. <https://doi.org/10.1007/s12668-023-01166-2>
- Hosseinzadeh K, Mardani MR, Paikar M, Hasibi A, Tavangar T, Nimafar M, Ganji DD, and Shafii MB (2023). Investigation of second grade viscoelastic non-Newtonian nanofluid flow on the curve stretching surface in presence of MHD. *Results in Engineering*, 17: 100838. <https://doi.org/10.1016/j.rineng.2022.100838>
- Hussain Z, Khan WA, Ali M, Waqas M, and Ashraf IM (2023). Chemically reactive magneto-bioconvection 3D flow of radiative Williamson nanofluid containing oxytactic moment of microorganisms. *Tribology International*, 189: 108934. <https://doi.org/10.1016/j.triboint.2023.108934>
- Jabeen K, Mushtaq M, Mushtaq T, and Muntazir RMA (2024). A numerical study of boundary layer flow of Williamson nanofluid in the presence of viscous dissipation, bioconvection, and activation energy. *Numerical Heat Transfer, Part A: Applications*, 85(3): 378-399. <https://doi.org/10.1080/10407782.2023.2187494>
- Jalili P, Narimisa H, Jalili B, Shateri A, and Ganji DD (2023). A novel analytical approach to micro-polar nanofluid thermal analysis in the presence of thermophoresis, Brownian motion and Hall currents. *Soft Computing*, 27(2): 677-689. <https://doi.org/10.1007/s00500-022-07643-2>



- Javaid M, Tahir M, Imran M, Baleanu D, Akgül A, and Imran MA (2022). Unsteady flow of fractional Burgers' fluid in a rotating annulus region with power law kernel. *Alexandria Engineering Journal*, 61(1): 17-27. <https://doi.org/10.1016/j.aej.2021.04.106>
- Khan SA, Hayat T, and Alsaedi A (2023). Bioconvection entropy optimized flow of Reiner-Rivlin nanofluid with motile microorganisms. *Alexandria Engineering Journal*, 79: 81-92. <https://doi.org/10.1016/j.aej.2023.07.069>
- Khan SU and Shehzad SA (2020). Electrical MHD Carreau nanofluid over porous oscillatory stretching surface with variable thermal conductivity: Applications of thermal extrusion system. *Physica A: Statistical Mechanics and its Applications*, 550: 124132. <https://doi.org/10.1016/j.physa.2020.124132>
- Li S, Ali F, Zaib A, Loganathan K, Eldin SM, Ijaz Khan M (2023a). Bioconvection effect in the Carreau nanofluid with Cattaneo-Christov heat flux using stagnation point flow in the entropy generation: Micromachines level study. *Open Physics*, 21(1): 20220228. <https://doi.org/10.1515/phys-2022-0228>
- Li Y, Majeed A, Ijaz N, Barghout K, Ali MR, Muhammad T (2023b). Melting thermal transportation in bioconvection Casson nanofluid flow over a nonlinear surface with motile microorganism: Application in bioprocessing thermal engineering. *Case Studies in Thermal Engineering*, 49: 103285. <https://doi.org/10.1016/j.csite.2023.103285>
- Maatoug S, Khan SU, Abbas T, Haq EU, Ghachem K, Kolsi L, and Abbasi A (2023). A lubricated stagnation point flow of nanofluid with heat and mass transfer phenomenon: Significance to hydraulic systems. *Journal of the Indian Chemical Society*, 100(1): 100825. <https://doi.org/10.1016/j.jics.2022.100825>
- Mabood F, Khan SU, and Thili I (2020). Numerical simulations for swimming of gyrotactic microorganisms with Williamson nanofluid featuring Wu's slip, activation energy and variable thermal conductivity. *Applied Nanoscience*, 13: 131-144. <https://doi.org/10.1007/s13204-020-01548-y>
- Mebarek-Oudina F and Chabani I (2023). Review on nano enhanced PCMs: insight on nePCM application in thermal management/storage systems. *Energies*, 16(3): 1066. <https://doi.org/10.3390/en16031066>
- Patil PM, Goudar B, and Momoniat E (2023). Magnetized bioconvective micropolar nanofluid flow over a wedge in the presence of oxytactic microorganisms. *Case Studies in Thermal Engineering*, 49: 103284. <https://doi.org/10.1016/j.csite.2023.103284>
- Rafique K, Mahmood Z, and Khan U (2023). Mathematical analysis of MHD hybrid nanofluid flow with variable viscosity and slip conditions over a stretching surface. *Materials Today Communications*, 36: 106692. <https://doi.org/10.1016/j.mtcomm.2023.106692>
- Shamshuddin MD, Shahzad F, Jamshed W, Bég OA, Eid MR, and Bég TA (2023). Thermo-solutal stratification and chemical reaction effects on radiative magnetized nanofluid flow along an exponentially stretching sensor plate: Computational analysis. *Journal of Magnetism and Magnetic Materials*, 565: 170286. <https://doi.org/10.1016/j.jmmm.2022.170286>
- Sharma BK, Kumawat C, and Bhatti MM (2023a). Optimizing energy generation in power-law nanofluid flow through curved arteries with gold nanoparticles. *Numerical Heat Transfer, Part A: Applications*, 85(18): 3058-3090. <https://doi.org/10.1080/10407782.2023.2232123>
- Sharma BK, Sharma P, Mishra NK, Noeiaghdam S, and Fernandez-Gamiz U (2023b). Bayesian regularization networks for micropolar ternary hybrid nanofluid flow of blood with homogeneous and heterogeneous reactions: Entropy generation optimization. *Alexandria Engineering Journal*, 77: 127-148. <https://doi.org/10.1016/j.aej.2023.06.080>
- Sheikholeslami M, Khalili Z, Scardi P, and Ataollahi N (2023). Concentrated solar photovoltaic cell equipped with thermoelectric layer in presence of nanofluid flow within porous heat sink: Impact of dust accumulation. *Sustainable Cities and Society*, 98: 104866. <https://doi.org/10.1016/j.scs.2023.104866>
- Zheng LC, Jin X, Zhang XX, and Zhang JH (2013). Unsteady heat and mass transfer in MHD flow over an oscillatory stretching surface with Soret and Dufour effects. *Acta Mechanica Sinica*, 29(5): 667-675. <https://doi.org/10.1007/s10409-013-0066-6>