

## Comparison of machine learning techniques for rainfall-runoff modeling in Punpun river basin, India



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### ABSTRACT

Machine learning (ML) models have emerged as potential methods for rainfall-runoff modeling in recent decades. The appeal of ML models for such applications is owing to their competitive performance when compared to alternative approaches, ease of application, and lack of rigorous distributional assumptions, among other attributes. Despite the promising results, most ML models for rainfall-runoff applications have been limited to areas where rainfall is the primary source of runoff. The potential of Random Forest (RF), a popular ML method, for rainfall-runoff prediction in the Punpun river basin, India, is investigated in this paper. The correlation coefficient (R), Root mean squared error (RMSE), Mean absolute error (MAE), and Nash–Sutcliffe efficiency (NSE) are four statistical metrics used to compare RF performance to that of alternative ML models. Model evaluation metrics indicate that RF outperforms all others. In the RF model, we got the best NSE score of 0.795. These findings offer new perspectives on how to apply RF-based rainfall-runoff modeling effectively.

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### 1. Introduction

Precise rainfall-runoff modeling is a key factor for effective water resources management and planning. It has been scientifically shown that the rainfall-runoff modeling of the river system is a challenging task due to physical processes and natural changes associated with the river system (Mohammadi, 2021). Because of the complex relationship between rainfall and runoff, accurate runoff estimation is always a difficult problem for hydrologists. Changes in river runoff are influenced by a variety of meteorological factors, including evapotranspiration, solar radiation, wind speed, air temperature, and catchment-specific characteristics, such as topography, shape, slope, altitude, soil type, land cover, and soil moisture-holding capacity, among others. Data on all of these factors is normally necessary for the successful running of rainfall-runoff models, which is a complex and challenging task, especially in developing nations with sparsely gauged catchments.

Due to the relatively low input data requirements, black-box models are chosen over conceptual and physically based models for modeling rainfall-runoff processes when reliable data on the aforementioned meteorological and site-specific parameters are not available. For modeling such complex nonlinear and nonstationary processes, ML models, such as artificial neural network (ANN) based, fuzzy-based, and regression-based machine learning (ML) models have been applied successfully in recent years.

Over the past decade, ML techniques have gained immense popularity in hydrology research. ML techniques have been successfully implemented for various hydrological applications for example flood modeling (Mosavi et al., 2018; Janizadeh et al., 2019) drought assessment (Feng et al., 2019; Shamshirband et al., 2020; Rhee and Im, 2017), water demand studies (Villarin and Rodriguez-Galiano, 2019; Xenochristou et al., 2021) rainfall modeling (Cramer et al., 2017; Basha et al., 2020), runoff modeling (Kumar et al., 2019; Taşar et al., 2019). Some of the ML models specifically used for rainfall-runoff modeling include ANN (Sudheer et al., 2002; Srinivasulu and Jain, 2006), adaptive neuro-fuzzy inference system or adaptive network-based fuzzy inference system (ANFIS) (Nourani and Komasi, 2013; Talei et al., 2010), multivariate adaptive regression splines model (MARS) (Sharda et al., 2008) and M5 model tree (M5Tree) (Adnan et al., 2021; Nourani et al., 2019), support vector regression (SVR) (Hosseini and Mahjouri, 2016;

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Sedighi et al., 2016). Extreme learning machine (ELM) (Roushangar et al., 2018), Group Method of Data Handling (GMDH) (Al-Juboori, 2022).

Among the decades-old regression-based ML models, the random forest (RF) regression model has been successfully used in many hydrological applications. This is a unique comparative study for the selected study area as we have compared six ML algorithms for rainfall-runoff modeling in the Punpun river basin of India.

## 2. Study area and data collection

The Punpun river basin is located on the southern bank of the Ganga River, with latitudes of 24 11' and 25 25' N and longitudes of 84 9' and 85 20' E. (Fig. 1). The Punpun River is surrounded by the west by the Sone River and the east by the Kiul-Harohar-

Falgu river system. The Punpun River, which originates in the Chhotanagpur hills of Jharkhand's Palamu district, is mostly a rain-fed river. It runs for 232 kilometers before joining the Ganga as a right bank tributary in the Fatuha region, 25 kilometers downstream of Patna. The Punpun River Basin, with its basin area of 8530 km<sup>2</sup>, has been chosen for this investigation. In the Punpun river basin, the average annual rainfall is between 960mm to 1020 mm.

Daily rainfall gridded data of 30 years i.e., from 1991 to 2020 have been obtained IMD website (www.imdpune.gov.in), for ten grid points of grid size 0.25×0.25, and monthly rainfall data has been calculated for the above grid points. The monthly discharge data of 30 years i.e., from 1991 to 2020 for the Sripalpur gauging site has been collected from Central Water Commission (CWC), Patna.

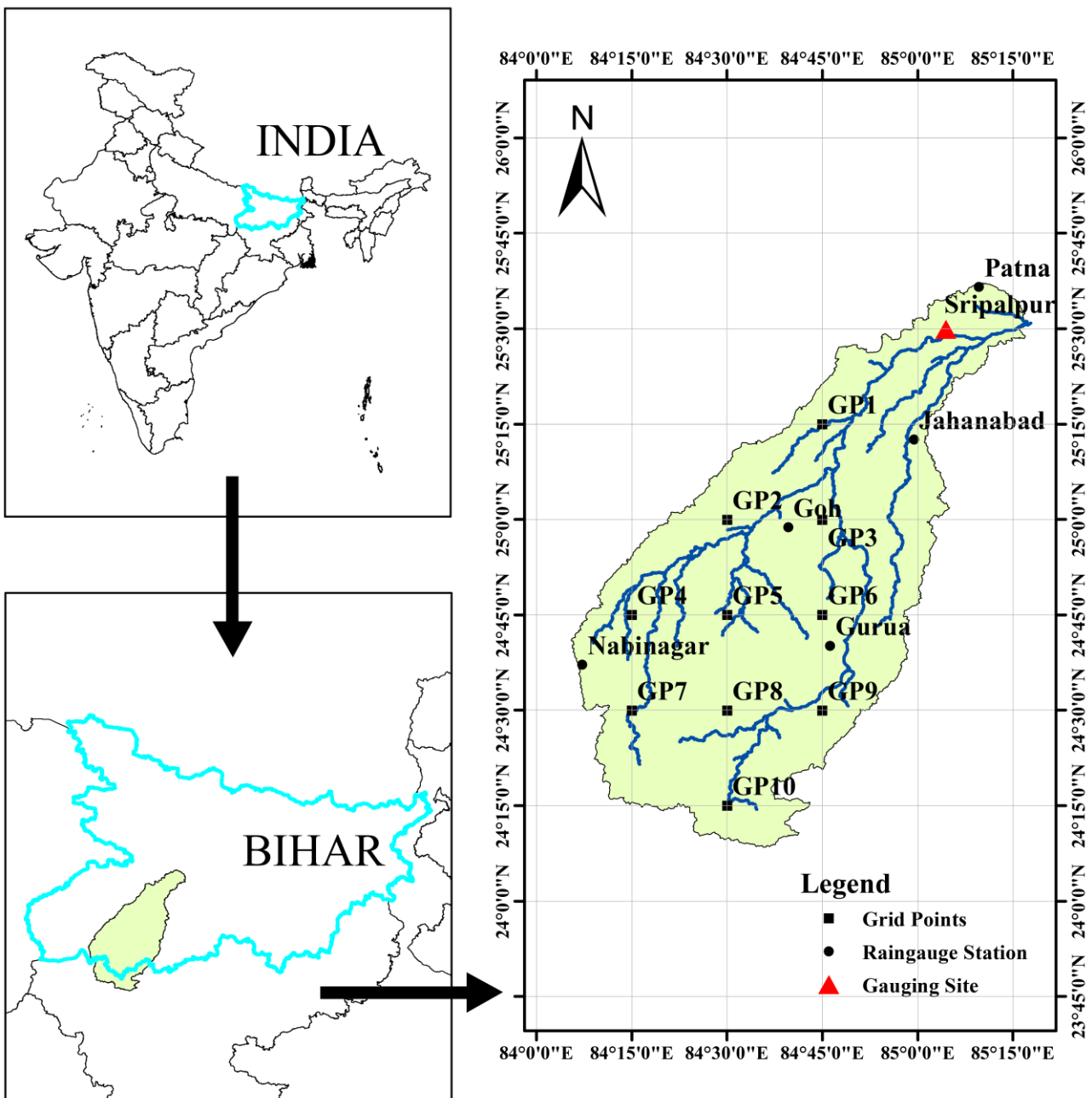


Fig. 1: Map showing the location of the Punpun river basin

### 3. Methodology

#### 3.1. ML approaches for rainfall-runoff modeling

Different machine-learning model approaches were utilized to illustrate each model's accuracy to estimate the runoff.

#### 3.2. Multiple linear regression (MLR)

MLR is a popular ML technique for regression problems. One independent variable is present in basic linear regression, and the model must establish a linear relationship between it and the dependent variable. In MLR, on the other hand, the model must consider multiple independent variables to find a relationship. The MLR approach is employed when the response variable is affected by more than one predictor variable.

Furthermore, MLR is an extension of Simple Linear Regression in that it predicts the response variable using more than one predictor variable. The equation of MLR can be defined as follows (Niu et al., 2019).

$$y = b_0 + b_1x_1 + b_2x_2 + b_3x_3 \dots \dots + b_nx_n \quad (1)$$

where,  $b_0$  is the intercept,  $b_1, b_2, b_3, \dots, b_n$  are coefficients or slopes of the independent variables  $x_1, x_2, x_3, \dots, x_n$  and  $y$  is the dependent variable.

#### 3.3. Least absolute shrinkage and selection operator (LASSO)

Tibshirani (1996) first presented the LASSO regression (LR) model. LASSO is a linear regression-based strategy that uses a shrinking process to confine the sum of the absolute values of the model parameters; as a result, the sum must be less than a predetermined number (Upper bound). The LR algorithm recommends simple, sparse models (models with fewer parameters), which are well-suited for models or data with high levels of multicollinearity or when we want to automate certain parts of model selection, such as variable selection or parameter elimination, using feature engineering. The LR algorithm employs the L1 regularization technique and is used when there are a large number of features because it automatically performs feature selection.

#### 3.4. Ridge regression (RR)

In ML, RR is another type of regression procedure that is used when there is a high correlation between the independent variables or model parameters (Shariff and Duzan, 2018). The least-square estimates evaluate unbiased values as the correlation value increases. However, if the dataset's collinearity is very high, there may be some bias value. As a result, we include a bias matrix in the RR algorithm equation. It is a useful regression method

in which the model is less susceptible to overfitting and thus works well even with small datasets.

#### 3.5. Polynomial regression (PR)

PR is a type of regression analysis in which the relationship between the independent and dependent variables is represented by an nth-degree polynomial. The least-squares method is commonly used to fit PR models (Maulud and Abdulazeez, 2020) According to the Gauss-Markov Theorem, the least-square method minimizes the variance of the coefficients. PR is a subset of Linear Regression in which the data is fitted with a polynomial equation with a curvilinear relationship between the dependent and independent variables. The relationship between the independent and dependent variables in the data set does not have to be linear for PR to work. This is also one of the main differences between Linear and PR. PR is generally used when the linear regression model does not capture the points in the data and the linear regression fails in describing the best result clearly.

#### 3.6. Support vector machine (SVR)

SVM was introduced by Vapnik (1995) based on supervised learning methods for classification and regression problems that analyze data and recognize patterns. The SVM learning system employs a hypothesis space of linear functions in a high dimensional feature space, which has been trained with an optimization theory learning algorithm that implements a statistical learning theory learning bias and structural risk minimization principle. In this present study, SVM is used for regression analysis therefore its SVR. SVR for regression is defined by the following equations.

Considering a set of training data  $\{(x_1, y_1), \dots, (x_n, y_n)\}$ , where  $x_i \in R^n$ ,  $y_i \in R$ , the decision function is represented by  $f(x) = w^T \phi(x) + b$ , with respect to  $w \in R^n$ ,  $b \in R$ , where  $f$  denotes a nonlinear transformation from  $R^n$  to a high-dimensional space. The primal optimization problem is given by:

$$\text{Minimize } R_{reg}(f) = \frac{1}{2} \|w\|^2 + c(\sum_{i=1}^n |y - f(x)|_\epsilon) \quad (2)$$

#### 3.7. RF

RF was introduced by Breiman (2001). RF is a supervised ML algorithm and also an ensemble ML technique for classification and regression that works by building a large number of decision trees. The principles behind ensemble learning techniques are based on the idea that it outperforms other ML algorithms in terms of accuracy because the combination of predictions outperforms any single constituent model. Distinct decision trees in RF tend to learn highly irregular patterns, i.e. to overfit their training data sets. The goal of RF is to minimize prediction variance by averaging multiple decision

trees trained on different parts of the same training data set. RF modeling is suitable for simulating the nonlinear effect of variables. It can handle complex variable interactions and is unaffected by multicollinearity. The RF can evaluate the effects of all instructive variables at the same time and automatically ranks their importance in descending order. Because the generalization error in RF converges as the number of trees surges, the RF does not overfit the data.

**4. Model development**

The selection of appropriate input variables in hydrological modeling studies would be critical in their applications. We developed hydrological model

strategies that predict outputs based on past rainfall and runoff data. As a result, four input data combinations for runoff record periods were prepared as shown in Table 1.

**4.1. Assessment of model performances**

Many techniques are recommended for the assessment of model performance in the literature. However, we used 4 performance evaluation criteria used in this study are shown in Table 2. In Table 2,  $Q_{obs}$  is observed runoff;  $Q_{for}$  is forecasted runoff;  $\bar{Q}_{obs}$  is average observed;  $\bar{Q}_{for}$  is average forecasted  $Q$ ;  $N$  is number of data points (70% for training and 30% for testing of the data).

**Table 1:** Input data combination

Combination	Model input	Model output
Combination_1	rainfall(t-1), runoff(t-1), rainfall(t)	runoff(t)
Combination_2	rainfall(t-1), rainfall(t)	runoff(t)
Combination_3	rainfall(t-2), runoff(t-2), rainfall(t-1), runoff(t-1), rainfall(t)	runoff(t)
Combination_4	rainfall(t-2), runoff(t-2), rainfall(t-1), rainfall(t)	runoff(t)

t represents the current month; t-1 represents the one month back and so on

**Table 2:** Performance evaluation parameters

Statistical measures	Formula	Range	Optimum value
Coefficient of correlation (R)	$R = \frac{\sum_{i=1}^N (Q_{obs} - \bar{Q}_{obs})(Q_{for} - \bar{Q}_{for})}{\sqrt{\sum_{i=1}^N (Q_{obs} - \bar{Q}_{obs})^2 (Q_{for} - \bar{Q}_{for})^2}}$	-1to1	0.8
Root mean square error (RMSE)	$RMSE = \sqrt{\frac{\sum_{i=1}^N (Q_{obs} - Q_{for})^2}{N}}$	The optimal value is 0	0
Nash-Sutcliffe efficiency (NSE)	$NSE = 1 - \left[ \frac{\sum_{i=1}^N (Q_{obs} - Q_{for})^2}{\sum_{i=1}^N (Q_{obs} - \bar{Q}_{obs})^2} \right]$	$-\infty$ to 1	1
Mean absolute error (MAE)	$MAE = \frac{1}{N} \sum_{i=1}^N  Q_{obs} - Q_{for} $	The optimal value is 0	0

**5. Results and discussion**

This section represents and discusses the case study's obtained results using the proposed ml models. Table 1 shows the different combinations of rainfall and runoff models. The models were built using 70% of the dataset for training and the remaining 30% for testing. All developed models have undergone 10-fold cross-validation. Model evaluation metrics suggest RF performs among all. We obtained the best NSE scores in the RF model i.e., 0.795 for combination\_1 which is followed by SVR (NSE=0.858) for the same combination. A comparative study of the best combination of each regression method has been shown in Fig. 2 for test data.

Table 3 shows that combination\_1 and combination\_2 models performed better than combination\_3 and combination\_4 in all the ML techniques except PR used in this study. In this study, the PR model developed is a second-degree polynomial model. Some authors give more priority to NSE and MAE matrices over R and RMSE for model selection because the former is less sensitive to extreme values. Further studies reported NSE is a normalized statistic that determines the relative

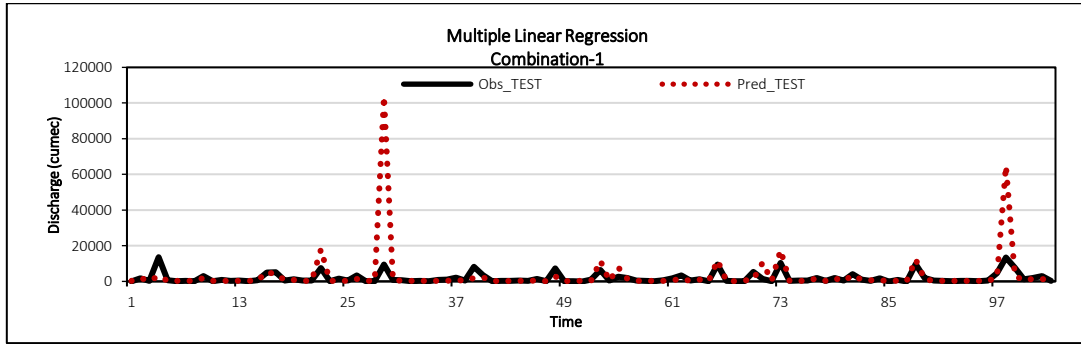
magnitude of the residual variance compared to the measured data variance.

These results presented provide new insights for the effective application of RF-based rainfall-runoff modeling.

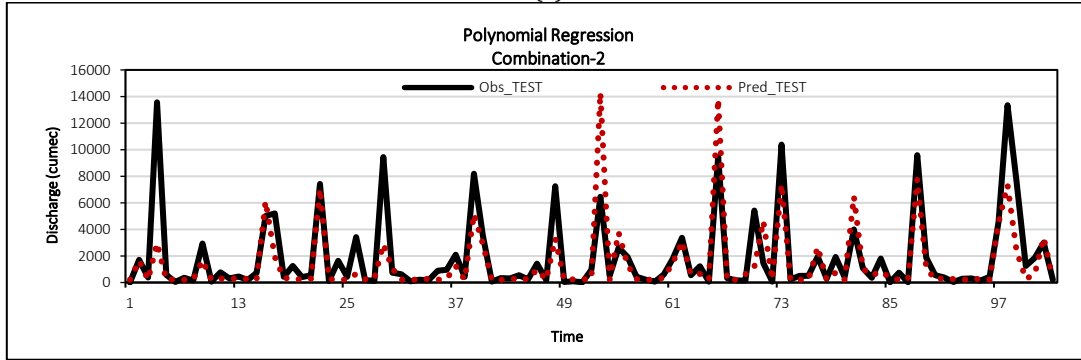
**6. Conclusion**

The research focused on the applicability of RF ML methods for rainfall-runoff modeling and compared the results to those of other ML algorithms. RF methods were implemented with several input scenarios, including previous rainfall and runoff data from the Punpun River basin in India.

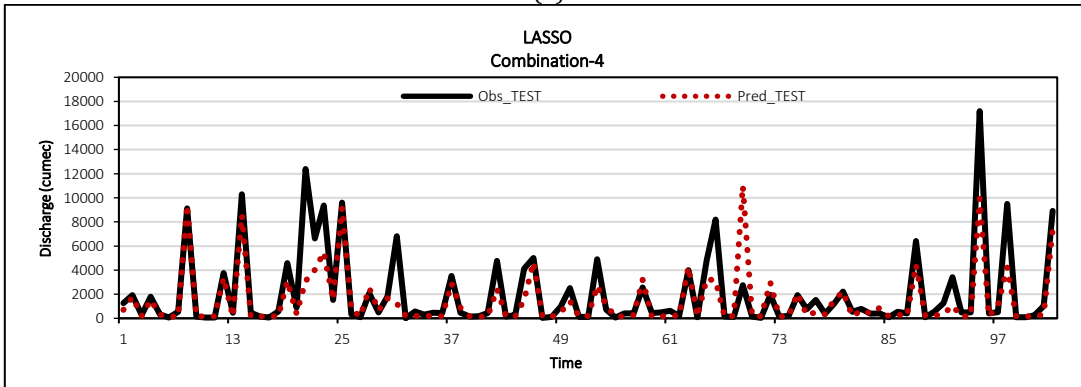
The RF model was developed using four different combinations of rainfall and runoff, and its results were compared to those of various machine-learning models. Given the Punpun river system's current and future vulnerabilities due to erratic rainfall, skilled rainfall-runoff modeling can have significant implications. RF and RF-based algorithms continue to gain popularity in hydrological studies due to their practical applications. Further study can be done using a coupled model and with combinations sorted by input selector techniques.



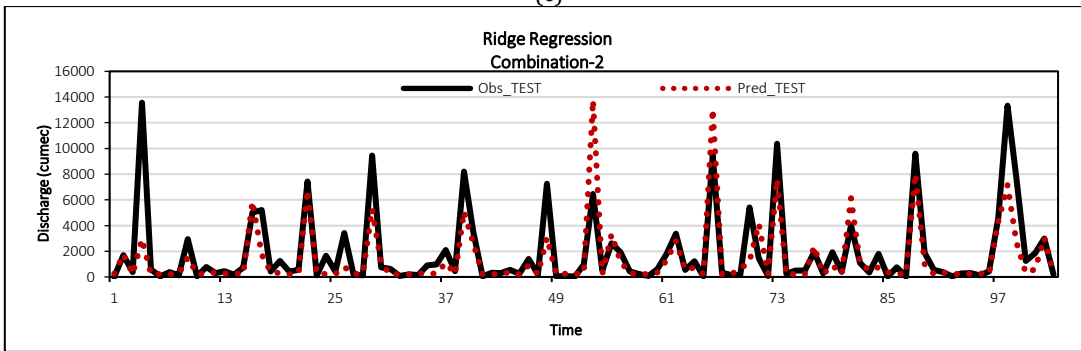
(a)



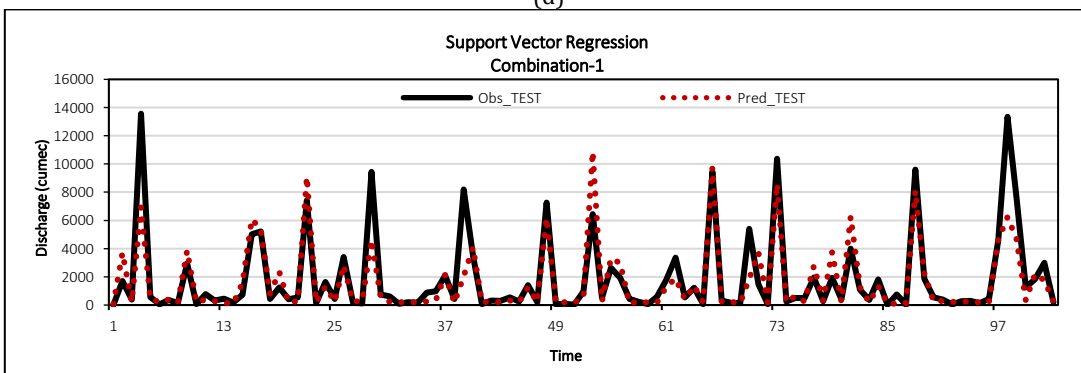
(b)



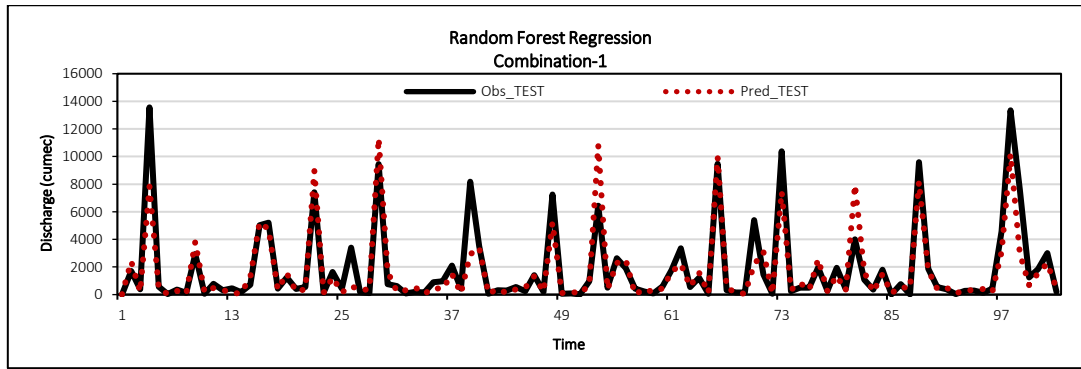
(c)



(d)



(e)



(f)

Fig. 2: Graphical representation of best combination for different regression methods (a) MLR (b) PR (c) LR (d) RR (e) SVR, and (f) RF

Table 3: Shows the error statistics

		Training				Testing			
		R	RMSE(m <sup>3</sup> /s)	NSE	MAE	R	RMSE(m <sup>3</sup> /s)	NSE	MAE
MLR	Combination_1	0.69	4257.947	-0.752	1484.582	0.577	10828.6	-12.654	2449.41
	Combination_2	0.757	2803.36	0.241	1197.61	0.366	17978.11	-36.637	2656.296
	Combination_3	-0.021	6199.01	-2.702	2870.076	-0.021	5461.733	-2.474	2848.476
	Combination_4	-0.02	6206.52	-2.711	2871.31	-0.021	5429.685	-2.433	2837.801
PR	Combination_1	0.792	2409.49	0.439	1044.866	0.668	3278.537	-0.252	1349.06
	Combination_2	0.692	2906	0.184	1081.793	0.758	1989.975	0.539	951.241
	Combination_3	-0.008	5491.13	-1.905	2849.435	-0.004	4015.517	-0.878	2401.467
LR	Combination_4	0.008	5586.45	-2.007	2784.195	0	3807.61	-0.688	2357.897
	Combination_1	0.037	4983.86	-1.53	2807.163	0.1	4937.731	-1.457	2744.796
	Combination_2	0.04	4884.23	-1.43	2645.435	0.155	3716.545	-0.392	2175.494
RR	Combination_3	0.786	2561.59	0.332	943.648	0.776	2063.724	0.571	912.739
	Combination_4	0.751	2841	0.178	978.053	0.828	1869.023	0.648	845.011
	Combination_1	0.781	2451.11	0.42	1013.918	0.684	2925.639	0.003	1211.204
SVR	Combination_2	0.704	2788.54	0.249	1058.059	0.786	1880.803	0.588	907.876
	Combination_3	0.001	5365.96	-1.774	2801.093	-0.017	3890.922	-0.763	2357.201
	Combination_4	0.01	5418.149	-1.828	2753.792	-0.006	3771.689	-0.657	2331.014
RF	Combination_1	0.923	1258.79	0.847	612.156	0.858	1523.729	0.73	731.803
	Combination_2	0.876	1581.58	0.758	768.886	0.84	1627.469	0.692	783.317
	Combination_3	0.032	4247.81	-0.739	2583.252	-0.007	3818.672	-0.698	2396.982
RF	Combination_4	0.037	4268.52	-0.756	2591.426	-0.033	3947.262	-0.814	2471.34
	Combination_1	0.978	774.798	0.942	339.094	0.894	1326.147	0.795	663.822
	Combination_2	0.964	926.955	0.917	405.262	0.835	1648.898	0.683	825.167
RF	Combination_3	0.009	4250.63	-0.741	2620.312	-0.033	3901.616	-0.773	2460.745
	Combination_4	0.019	4192.31	-0.693	2583.135	-0.025	3757.663	-0.644	2395.793

**Compliance with ethical standards**

**Conflict of interest**

The author(s) declared no potential conflicts of interest with respect to the research, authorship, and/or publication of this article.

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