

# Novel assessment of power system reserve-based on the reliability and quality levels



Badr M. Alshammari <sup>1,\*</sup>, Abdullah M. Al-Shaalan <sup>2</sup>

<sup>1</sup>Department of Electrical Engineering, College of Engineering, University of Hail, Hail, Saudi Arabia

<sup>2</sup>Department of Electrical Engineering, College of Engineering, King Saud University, Riyadh, Saudi Arabia

## ARTICLE INFO

### Article history:

Received 12 December 2019

Received in revised form

1 March 2020

Accepted 2 March 2020

### Keywords:

Power systems

Reliability evaluation

Performance quality

Probabilistic analysis

## ABSTRACT

This paper presents a novel framework for the assessment of reliability and quality indices and the associated reserve levels in electric power systems. The developed technique takes into account the variations of demand and contingencies, which occur randomly, causing some units of generation, and/or transmission capacities to be lost. The evaluated reliability and quality measures, which are essential to assess the reserve capabilities of the power system for various operating scenarios, are probabilistic in nature. In fact, the value of demand levels, the capacity of the generation and transmission capacities are known with absolute certainty. The assessment of reliability and quality indices, in this paper, are subject to random variations and, consequently, as well as the calculated reliability indices are all subject to random variations where only expected values of these indices can be evaluated. This paper presents a novel assessment of the power system reserve-based on the reliability and quality levels. Practical applications are additionally exhibited, for demonstration purposes, to the Saudi electricity power networks.

© 2020 The Authors. Published by IASE. This is an open access article under the CC BY-NC-ND license (<http://creativecommons.org/licenses/by-nc-nd/4.0/>).

## 1. Introduction

Maintaining a continuous and sufficient power supply to the customers at a reasonable cost is the prime objective of electric power companies around the world. In this regard, power system cost-effectiveness, security, adequacy, and reliability analyses have become a significant concern in today's highly-competitive business environment of power utility planning and operations (Zhao et al., 2009; El-Kady et al., 1985; 1986). In a recent paper by the authors (El-Kady and Alshammari, 2011), a novel framework was developed and applied for assessment of reliability and quality performance levels in real-life power systems with practical large-scale sizes. The new assessment methodology is based on three metaphors (dimensions) representing the relationship between available generation capacities and required demand levels. The first metaphor defines whether or not the capacity exists, the second metaphor defines

whether or not the capacity is needed, and the last metaphor defines whether or not the capacity can reach (delivered to) the demand. The eight possible combinations associated with the 0/1 (Yes/No) values of the three metaphors would, in turn, define a set of powerful system-wide performance quality measures relating to generation deficiency, redundancy, bottling, etc.

To determine reliability is of great importance to power plants or energy producers from the perspective of consumers or distribution companies (Akhavain and Firuzabad, 2011). The reliability of composite generation and transmission systems plays a crucial role in system evaluation. It provides planners and decision-makers with valuable and intuitively interpretable information (Goel and Low, 2001). However, a review that systematically gathers such work in this area is still needed.

The developed reliability and performance quality indices were deterministic in nature (de Jong et al., 2017; Alshammari, 2019; Pérez-Londoño et al., 2017). That is, they represent one operating state (a snapshot of the system conditions) in which the required demand, as well as the generation and transmission capacities, are known with 100% certainty (Choi et al., 2007; Jirutitijaroen and Singh, 2008; Billinton and Huang, 2008). In real life, however, load variations occur randomly so as the contingencies which cause some generation and/or

\* Corresponding Author.

Email Address: [bms.alshammari@uoh.edu.sa](mailto:bms.alshammari@uoh.edu.sa) (B. M. Alshammari)

<https://doi.org/10.21833/ijaas.2020.06.002>

Corresponding author's ORCID profile:

<https://orcid.org/0000-0001-6819-3695>

2313-626X/© 2020 The Authors. Published by IASE.

This is an open access article under the CC BY-NC-ND license

(<http://creativecommons.org/licenses/by-nc-nd/4.0/>)

transmission capacities to be lost (become unavailable). In other words, neither the load levels nor the generation or transmission capacities are known with absolute certainty. They are rather subject to random variations and, consequently, the calculated reliability and performance quality indices are all subject to random variations where only expected values of these indices can be evaluated. Methods for computing probabilistic contingency-based reliability and performance quality indices have previously been published in the literature (Jirutitijaroen and Singh, 2008; Alshammari, 2018; Billinton and Huang, 2008; El-Kady et al., 2007; Kolisnyk et al., 2019; Cheon, 2019; Wilson and Wang, 2019). These methods are based on a combined contingency analysis and reliability evaluation scheme, which integrates both the contingency effect and its probability of occurrence into one routine of study. In the present research work, a similar analysis will be used to compute the expected values of different system reliability and performance quality indices. In this context, a “contingency scenario” or a system “demand level” is regarded, in a more general sense, as a “state,” which occurs with a certain probability and represents a given demand value and availability pattern of various capacities in the system.

On the other hand, the impact of transmission line loading on the reliability of the power network was investigated (Teh et al., 2017). This will assist power system operators in taking a cost-effective decision in regards to the management of the transmission network.

The work of this paper presents a major extension to the previously published work (El-Kady and Alshammari, 2011), by developing theory and formulas for computing the expected values of different system reliability and performance quality indices. In this context, a “contingency scenario” or a system “demand level” is regarded, in a more general sense, as a “state,” which occurs with a certain probability and represents a given demand value and availability pattern of various capacities in the system. This paper provides a practical and meaningful methodology for the real-life assessment of power system reliability and performance quality levels. Practical applications are also presented in the Saudi electricity power grid.

## 2. Power system quality assessment

### 2.1. Performance quality framework

In the framework presented in El-Kady and Alshammari (2011), three metaphors (dimensions) were introduced to represent the relationship between certain system generation capacity and demand. These metaphors relate to the following demand fulfillment issues:

- a) Need of capacity for demand fulfillment
- b) Existence of capacity (availability for demand fulfillment)

### c) Ability of capacity to reach the demand

The first metaphor defines whether or not the capacity is needed, the second metaphor defines whether or not the capacity exists, and the last metaphor defines whether or not the capacity can reach (delivered to) the demand. The eight possible combinations associated with the 0/1 (Yes/No) values of the three metaphors would, in turn, define a set of powerful system-wide performance quality measures, namely:

- 1) **Utilized:** A given capacity is said to be **utilized** if it is *needed* (for demand fulfillment), *exists*, and *can reach* the demand.
- 2) **Bottled:** A given capacity is said to be **bottled** if it is *needed* (for demand fulfillment) and *exists*, but *cannot reach* the demand.
- 3) **Shortfall:** A given capacity is said to be **shortfall** if it is *needed* (for demand fulfillment) and, anyhow, *does not exist* and *can reach* the demand.
- 4) **Deficit:** A given capacity is said to be a **deficit** if it is *needed* (for demand fulfillment) but, however, *does not exist* and *cannot reach* the demand.
- 5) **Surplus:** A given capacity is said to be **surplus** if it is *not needed* (for demand fulfillment), although it *exists* and *can reach* the demand.
- 6) **Redundant:** A given capacity is said to be **redundant** if it is *not needed* (for Demand fulfillment) although *exists* but, anyhow, *cannot reach* the demand.
- 7) **Spared:** A given capacity is said to be **spared** if it is *not needed* (for demand fulfillment) and, anyhow, *does not exist* although it *can reach* the demand.
- 8) **Saved:** A given capacity is said to be **saved** if it is *no needed* (for demand fulfillment) and, anyhow, *does not exist* and *cannot reach* the demand.

We note here that the above performance quality measures are associated with different combinations (topples) of the three quality metaphors, namely, “existence,” “need” and “ability to reach the demand.” The corresponding quality state of a given capacity can be represented by a three-value expression of either a “Yes/No” or “1/0” type indicating the true/false value associated with each quality metaphor.

The evaluation of the above quality indices requires the knowledge of the following data types for the demand and various system facilities:

- a) The value of demand required to be supplied.
- b) The value of generation capacity as well as the maximum site capacity (the limit of a potential increase in existing generation capacity).
- c) The value of transmission capacity.

### 2.2. Linear program formulation

In the computational scheme of El-Kady and Alshammari (2011), the integrated system quality assessment is performed via solving a master linear

programming problem (El-Kady and Alshammari, 2012; Alshammari and El-Kady, 2012) in which a feasible power flow is established which minimizes the total system non-served load subject to capacity limits and flow equations. The master linear program, which utilizes the network bus incidence matrix  $\mathbf{A}$ , is formulated as:

$$\begin{aligned} \text{Minimize } f &= \sum_{l=1}^{n_L} (-P_l) \\ \text{With respect to } P_L, P_G \text{ and } P_T \\ \text{Such that} \\ AP_T &= \begin{bmatrix} -P_L \\ P_G \end{bmatrix} \\ P_L &\leq \bar{P}_L, -P_L \leq 0 \\ P_G &\leq \bar{P}_G, -P_G \leq 0 \\ P_T &\leq \bar{P}_T, -P_T \leq \bar{P}_T, \end{aligned} \quad (1a)$$

where in the above master linear program (Eq. 1a),  $\bar{P}_T$  is a vector of  $n_T$  elements representing transmission branch capacities;  $\bar{P}_L$  is a vector of  $n_L$  elements of peak bus loads;  $\bar{P}_G$ =vector of  $n_G$  elements are representing generator capacities.

Also, in Eq. 1a,  $P_L$ ,  $P_G$ , and  $P_T$  are  $n_L$ ,  $n_G$  and  $n_T$  column vectors representing the actual load bus powers (measured outward), generator bus powers (measured inwards), and transmission line powers (measured as per the network bus incidence matrix  $\mathbf{A}$ ), respectively. The solution of the above linear program provides a more realistic (less conservative) flow pattern in view of the fact that when load curtailments are anticipated, all system generation resources would be re-dispatched in such a way that minimizes such load cuts. The feasible flow pattern established from the Master Linear Program is then used to evaluate various integrated system quality indices through a set of closely related sub-problems.

### 2.3. Implementation mechanisms

For real-life power systems with practical sizes, the quality indices cannot be evaluated by inspection. An appropriate computerized scheme is needed in order to properly evaluate various quality indices according to their stated definitions. The master linear program presented before forms the bases for analyzing and evaluating the quality indices. For example, the Load Supply Reliability can be evaluated as follows:

$$LNS_l = \text{Load Not - Served at Bus } (l) = (\bar{P}_l - P_l^{(1)}) \quad (1b)$$

$$LNS = \text{Total System Load Not - Served} = \sum_{l=1}^{n_L} (\bar{P}_l - P_l^{(1)}), \quad (1c)$$

where, the busloads at the solution of the master linear program are termed as  $P_l^{(1)}$ , and denotes the solution load value at the bus (l).

On the other hand, generation quality indices are defined in terms of the previously defined "1/0" states indicating the (Needed, Exists, Can-reach) true/false values associated with each quality

metaphor. We shall use the symbol  $Q_{gijk}$  to indicate the generation quality index state. Also, in the following expressions, we shall use  $\text{Min}\{x, y, \dots, z\}$  to indicate the minimum of  $x, y, \dots, z$ . The notation  $< x$  will be used to denote  $\text{Max}\{0, x\}$ , that is the maximum of  $x$  and zero ( $= x$  if  $x > 0$ , or 0 otherwise). For example, the Utilized Generation Capacity index is given by:

$$\begin{aligned} Q_{g111} = \text{Utilized Capacity} &\equiv \\ \{\text{needed, exists, can reach}\} &= \sum_{i=1}^{n_L} (P_i^{(1)}). \end{aligned} \quad (1d)$$

Similarly, the Bottled Generation Capacity index is given by

$$\begin{aligned} Q_{g110} = \text{Bottled Capacity} &\equiv \\ \{\text{needed, exists, cannot reach}\} &= \\ \text{Min} \{[\sum_{l=1}^{n_L} (P_l) - \sum_{g=1}^{n_G} P_g^{(1)}], [\sum_{g=1}^{n_G} \text{Max}\{0, (\bar{P}_g - P_g^{(1)})\}]\}. \end{aligned} \quad (1e)$$

Also, the Surplus Generation Capacity ( $Q_{g011}$ ) is calculated as

$$\begin{aligned} Q_{g011} = \text{Surplus Capacity} &\equiv \\ \{\text{not needed, exists, can reach}\} &= \\ \text{Min} \{[\text{Max}\{0, (\sum_{g=1}^{n_G} \bar{P}_g - \sum_{l=1}^{n_L} \bar{P}_l)\}], \text{Max}\{0, (\sum_{g=1}^{n_G} \bar{P}_g - \sum_{l=1}^{n_L} \bar{P}_l)\}]\}, \end{aligned} \quad (1f)$$

where, the generation output values  $P_g$  are calculated at the solution of the linear program with open limits on the loads.

## 3. Probabilistic assessment

### 3.1. Probabilistic reliability indices

The power system can be described, for the purpose of composite reliability and performance quality assessment, by the three-component model, as shown in Fig. 1, in which generation, transmission, and load are considered as multi-state elements of the power system.

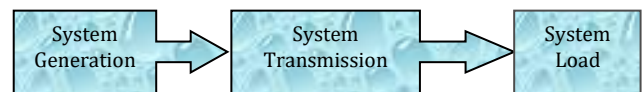


Fig. 1: System model reliability evaluation

For a given operating state  $m$ , the values of the network variables will be the solution of the maximum load-supply optimization problem described in the previous section. Also, let  $f_m$  be the probability of operating state  $m$  (the sum of  $f_m$  for all  $m$ , including base-case scenario is 1). Then, the following three system-wide reliability indices may be defined:

#### a) Loss of load probability

$$OLP = \sum_{m=1}^{M_c} LOLP^{(m)}, \quad (2a)$$

where,

$$LOLP^{(m)} = \text{Max}_l \{Y_l LOLP_l^{(m)}\}, \quad (2b)$$

represents the system loss of load probability for any operating state  $m$  (load level, loss of generation and/or transmission capacities) in the power grid,

$$LOLP_l^{(m)} = \lambda_l^m f_m, \quad (2c)$$

represents the loss of load probability at the bus  $\ell$  for operating state  $m$ ,

$$\lambda_l^{(m)} = \begin{cases} 0 & \text{if } P_l^{(m)} \leq P_l^o \\ 1 & \text{if } P_l^{(m)} > P_l^o \end{cases}, \quad (2d)$$

where,  $P_l^o$  denotes the scheduled (required) load at load bus  $\ell$ ,  $M_c$  denotes the number of all possible states.

### b) Expected load not-served

$$e(LNS) = \sum_{l=1}^{n_l} (eLNS_l), \quad (3a)$$

where,  $n_l$  is the number of load buses in the system,

$$(eLNS_l) = \sum_{m=1}^{M_c} (eLNS_l^{(m)}), \quad (3b)$$

represents the expected value of load not-served at bus  $\ell$ ,

$$(eLNS_l^{(m)}) = f_m LNS_l^{(m)}, \quad (3c)$$

represents the expected value of Load Not-Served at bus  $\ell$  for the operating state  $m$ , and  $LNS_l^{(m)}$  is Load not served at bus  $\ell$  for operating state  $m$ , which is obtained from the solution of the Eq. 1a.

### c) Expected energy not served

$$(eENS) = \sum_{l=1}^{n_l} (eENS_l), \quad (4a)$$

where,

$$(eENS_l) = \sum_{m=1}^{M_c} (eLNS_l^{(m)}), \quad (4b)$$

represents the expected value of energy not served at a bus  $\ell$ , and,

$$(eENS_l^{(m)}) = f_m ENS_l^{(m)}, \quad (4c)$$

represents the expected value of energy not served at the bus  $\ell$  for operating state  $m$ ,

$$ENS_l^{(m)} = T^{(m)} LNS_l^{(m)}, \quad (4d)$$

represents the energy not served at the bus  $\ell$  for operating state  $m$ , and  $T^{(m)}$  denotes the time duration of operating state  $m$ .

## 3.2. Probabilistic performance quality indices

Probabilistic performance quality indices can be calculated using the previously derived formulas based on the solution of the master linear program

(1) subject to random variations of system demand level as well as forced outages in various generation and transmission facilities. For example, the load variations, which are accounted for using the so-called “load-duration curves” can be used to calculate the expected value of the Load Not-Served (LNS), which is widely known as the Expected Load Not-Served (eLNS). On the other hand, the randomness in the generation and transmission capacity availability is accounted for using the so-called forced-outage rates (or availability rates) associated with various facilities. Consequently, the expected values of the performance quality indices  $Q_{g111}$ ,  $Q_{g110}$ ,  $Q_{g101}$ , etc., denoted by  $eQ_{g111}$ ,  $eQ_{g110}$ ,  $eQ_{g101}$ , etc., can be evaluated using the modeled randomness of the system load as well as the generation and transmission capacity availabilities.

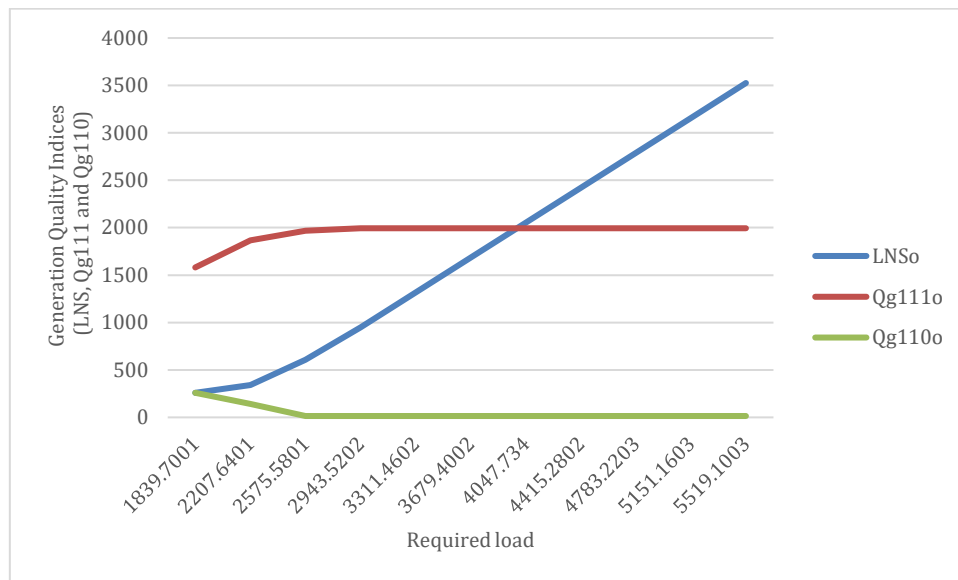
## 4. Applications to SEC power system

### 4.1. SEC quality performance indices

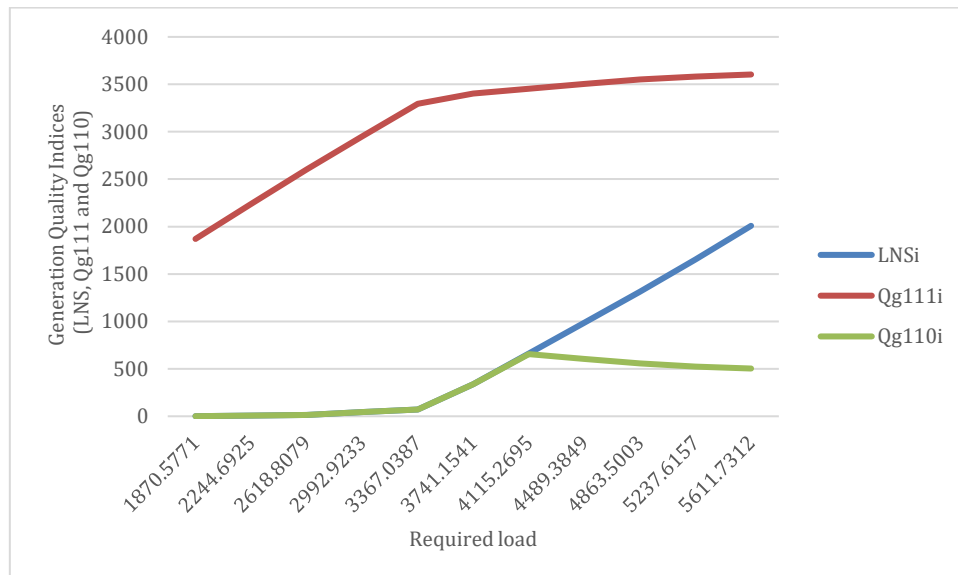
In a recently completed industry-supported study, applications were conducted on an efficient power system comprising a portion of the interconnected Saudi power grid. The power system consists of two main regions, namely the Central region and the Eastern region. The two systems are interconnected through two 380 kV and one 230 kV double-circuit lines. Four zones are identified in the present analysis, three in the Central region (Riyadh, Qassim, and Hail zones) and one in the Eastern region. In this application, three reliability and quality performance indices are considered, namely the system Load Not-Served (LNS), Utilized Generation Capacity ( $Q_{g111}$ ), and the Bottled Generation Capacity ( $Q_{g110}$ ). In the present work, a particular focus will be on Qassim and Hail zones for demonstration purposes. The system models used for these two zones are shown in Figs. 2 and 3, respectively. Table 1 outlines the network data in terms of generation and transmission facilities as well as system loads. Figs. 4 and 5, on the other hand, summarize the results of the performance quality measures applied to the SEC power system for various system status (isolated or connected) of each zone. In particular, Figs. 6 and 7 depict the variation of quality indices (LNS,  $Q_{g111}$ , and  $Q_{g110}$ ) with the required load level of the Qassim isolated and interconnected network, respectively. Figs. 9 and 10, on the other hand, show 3-dimensional graphs depicting the variation of Utilized Generation Capacity index  $Q_{g111}$  with both load and generation capacity levels of the Hail isolated and interconnected network, respectively. The results obtained reveal several essential observations. For example, the results obtained for the isolated network scenario of Qassim zone (Fig. 4) show that the Load Not-Served is non-zero even for relatively low demand levels as it increases continuously from 300 MW at a demand level of 1,840 MW to reach 2,400 MW when the demand level is 4,410 MW. This



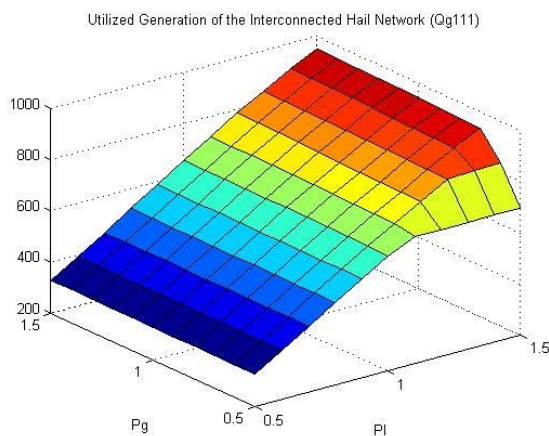




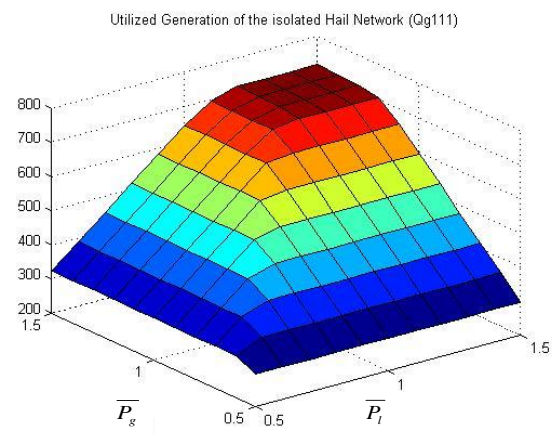
**Fig. 4:** Variation of quality indices ( $LNS$ ,  $Qg111$ , and  $Qg110$ ) with the required load level of the Qassim isolated network



**Fig. 5:** Variation of quality indices ( $LNS$ ,  $Qg111$ , and  $Qg110$ ) with the required load level of the Qassim interconnected network



**Fig. 6:** 3-dimensional graph showing the variation of utilized generation index  $Qg111$  with both load and generation capacity levels of the Hail isolated network



**Fig. 7:** 3-dimensional graph showing the variation of utilized generation index  $Qg111$  with both load and generation capacity levels of the Hail interconnected

Based on the actual load duration curve of Hail, shown in Fig. 8, the system load is assumed to have seven possible levels, namely 150 MW, 200 MW, 300 MW, 400 MW, 500 MW, 600 MW and 650 MW with probabilities of occurrence (calculated from the load duration curve) equal 0.009, 0.2, 0.314, 0.182, 0.045, 0.23 and 0.023, respectively.

Using the results of the probabilistic analysis of the Hail system, the discrete probability density functions of various reliability and performance quality indices can be evaluated and displayed. These discrete density functions show the overall probabilities of occurrence associated with certain values of the system performance indices.

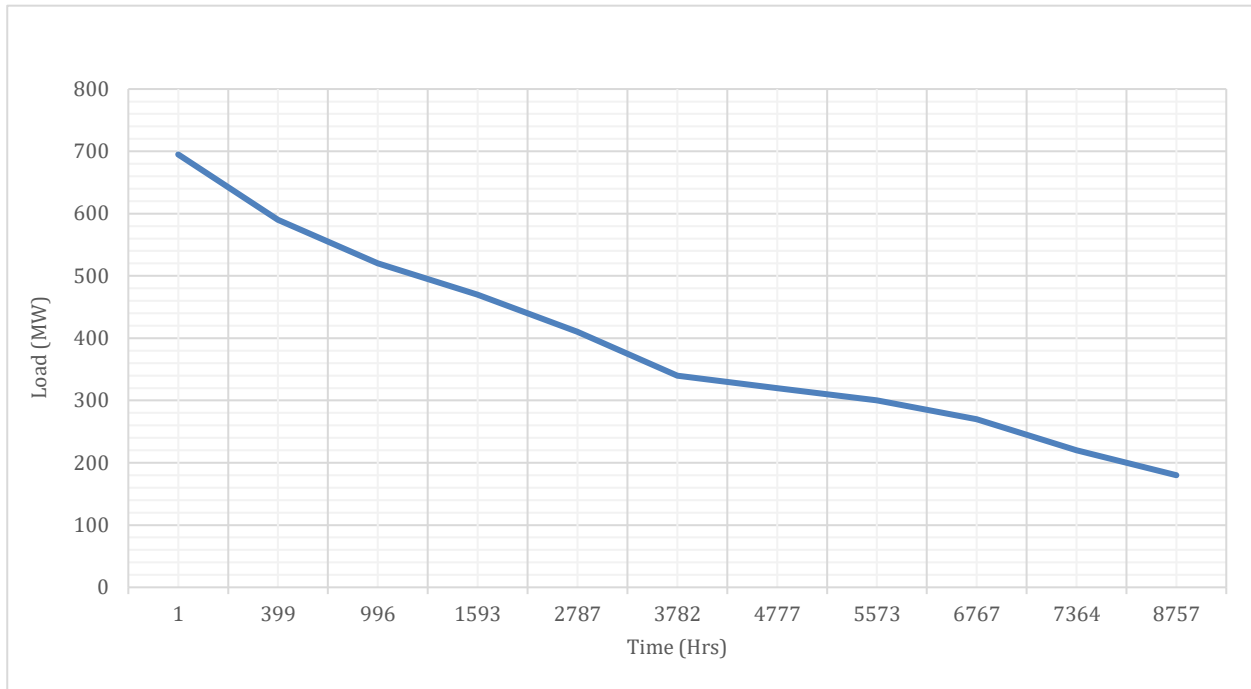


Fig. 8: Hail load duration curve

The probability density function of the Load Not Served (LNS) for the Hail network at a required load level 150 MW is depicted in Fig. 9. Also, Fig. 10 shows the probability density of the Surplus Generation Capacity ( $Q_{g011}$ ) at a load level of 200 MW.

Some valuable information can be drawn from the probability density functions of Figs. 9 and 10.

For example, the probability of Load Not Served (LNS) in Hail being zero when the required load level is 150 MW is 0.9387 (Fig. 9) while there is a probability of 0.0310 that the unsupplied load is equal to or greater than 25 MW. On the other hand, there is a probability of 0.92 that the Surplus Generation Capacity ( $Q_{g011}$ ) in Hail (at load level 200 MW) is equal to or greater than 1175 MW.

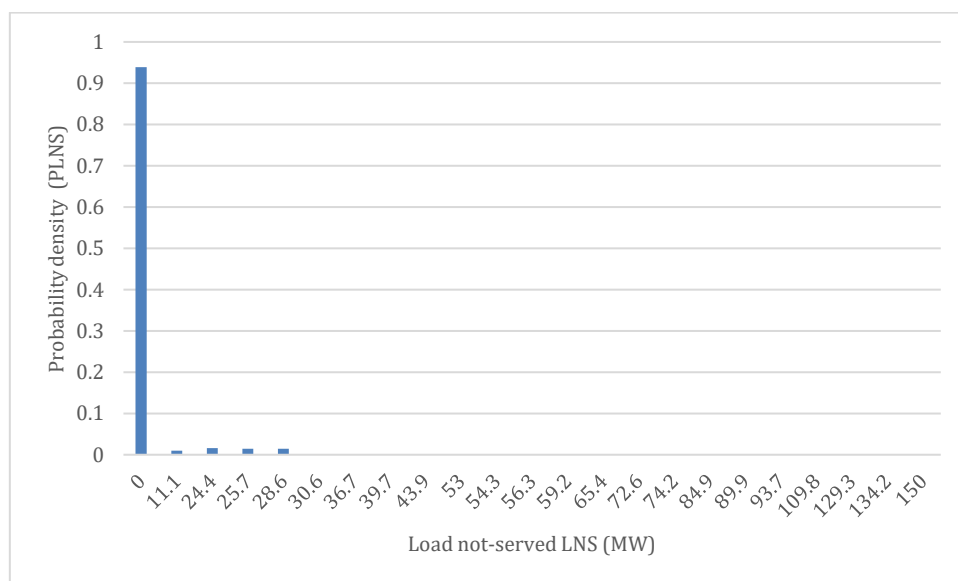
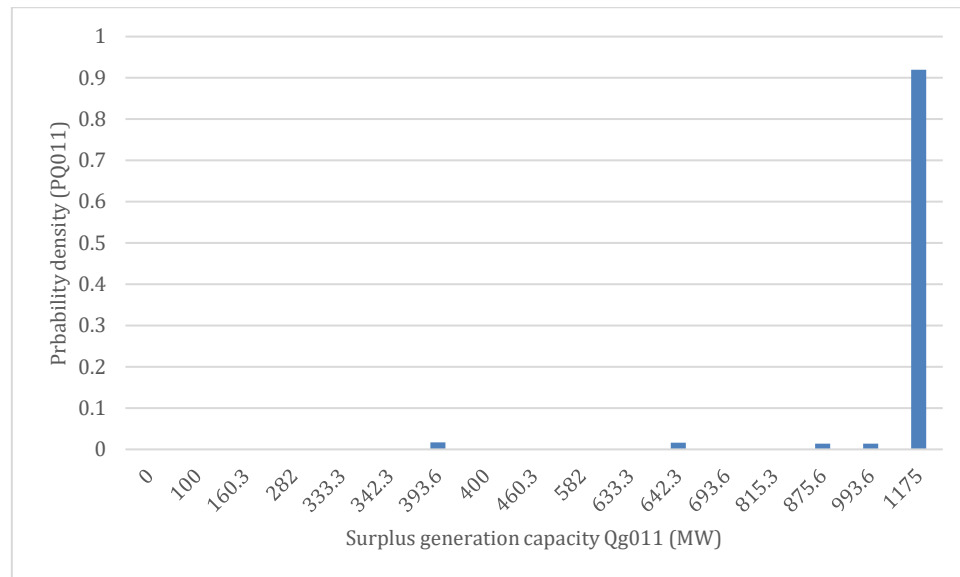


Fig. 9: Probability density of load not served (LNS) for Hail network at load 150 MW



**Fig. 10:** Probability density of surplus generation capacity ( $Q_{g011}$ ) for Hail network at load 200 MW

When all required load levels are considered with their respective probabilities of occurrence (as per the load duration curve), an overall estimate of the expected value of reliability and performance quality indices can be obtained, as shown in Table 2.

**Table 2:** Expedited values of reliability and performance quality indices for Hail network

Index	Expected Value
Load Not Served (LNS)	4.01 (MW)
Utilized Generation Capacity ( $Q_{g111}$ )	378.1 (MW)
Bottled Generation Capacity ( $Q_{g110}$ )	3.86 (MW)
Surplus Generation Capacity ( $Q_{g011}$ )	962.5 (MW)
Redundant Generation Capacity ( $Q_{g010}$ )	24.8 (MW)

The overall expected value of the Load Not Served (LNS) for Hail is 4.01 MW, which is less than 1% of the required load in Hail. On the other hand, the overall expected value of the Bottled Generation Capacity ( $Q_{g110}$ ) is 3.86 (MW), which again is less than 1% of the total Hail generation. It is also of interest to note that the overall expected value of the Utilized Generation Capacity ( $Q_{g111}$ ) is 378.1 (MW), which represents almost 64% of the total generation capacity in Hail. In other words, about 36% of Hail available generation capacity is expected to be unutilized. Recalling from Table 1 that the Hail generation capacity is 594 MW (base value) while the required base load is 655 MW, one may conclude that the 64% expected value for the utilized generation is a reflection of the relatively large variations of the required load during different periods of the year, as is evident from the load duration curve of Fig. 8.

## 5. Conclusion

This paper has presented the findings and results of a recent industry-supported study to assess the overall performance of power systems in terms of a pertinent set of reliability and quality measures. The work of this paper represents a significant extension to the previously published work by developing theory and formulas for computing the expected

values of different system reliability and performance quality indices.

The reliability and performance quality indices, when evaluated at a given load level and a certain scenario of available generation and transmission capacities, would provide an indication of system performance for only such a particular system condition (snapshot). However, the novel formulation presented in this paper can accommodate the randomness associated with the load level as well as the availability of generation and transmission capacities. In this case, expected values of reliability indices, such as the Expected Load Not-Served (eLNS), as well as the expected values of performance quality indices, such as Utilized Generation Capacity (eQg111), Bottled Generation Capacity (eQg110), Shortfall Generation Capacity (eQg101), Deficit Generation Capacity (eQg100), Surplus Generation Capacity (eQg011), Redundant Generation Capacity (eQg010), Spared Generation Capacity (eQg001) and Saved Generation Capacity (eQg000) can be calculated using the load duration curve as well as the availability rates of generation and transmission facilities in the system. The practical applications to large-scale portions of the Saudi power grid presented in the paper have demonstrated powerful features of the newly developed approach for performance assessment of power systems.

## Acknowledgment

This work was supported by the University of Hail.

## Compliance with ethical standards

## Conflict of interest

The authors declare that they have no conflict of interest.



## References

- Akhavein A and Firuzabad MF (2011). A heuristic-based approach for reliability importance assessment of energy producers. *Energy Policy*, 39(3): 1562-1568.  
<https://doi.org/10.1016/j.enpol.2010.12.030>
- Alshammari BM (2018). Integrated renewable energy and load management strategies in power systems. *International Journal of Advanced and Applied Sciences*, 5(6): 79-87.  
<https://doi.org/10.21833/ijaas.2018.06.012>
- Alshammari BM (2019). Evaluation of power system reliability levels for (N-1) outage contingency. *International Journal of Advanced and Applied Sciences*, 6(11): 68-74.  
<https://doi.org/10.21833/ijaas.2019.11.009>
- Alshammari BM and El-Kady MA (2012). Probabilistic assessment of power system performance quality. *Energy and Power Engineering*, 4(5): 372-379.  
<https://doi.org/10.4236/epe.2012.45049>
- Billinton R and Huang D (2008). Effects of load forecast uncertainty on bulk electric system reliability evaluation. *IEEE Transactions on Power Systems*, 23(2): 418-425.  
<https://doi.org/10.1109/TPWRS.2008.920078>
- Cheon IT (2019). On the plug-in electric vehicles effects investigation in electricity marketing. *Annals of Electrical and Electronic Engineering*, 2(5): 6-13.  
<https://doi.org/10.21833/AEEEE.2019.05.002>
- Choi J, Mount TD, and Thomas RJ (2007). Transmission expansion planning using contingency criteria. *IEEE Transactions on Power Systems*, 22(4): 2249-2261.  
<https://doi.org/10.1109/TPWRS.2007.908478>
- de Jong M, Papaefthymiou G, and Palensky P (2017). A framework for incorporation of infeed uncertainty in power system risk-based security assessment. *IEEE Transactions on Power Systems*, 33(1): 613-621.  
<https://doi.org/10.1109/TPWRS.2017.2687983>
- El-Kady M, Alaskar B, Shaalan A, and Al-Shammri B (2007). Composite reliability and quality assessment of interconnected power systems. *International Journal for Computation and Mathematic in Electrical and Electronic Engineering* 26: 7-21.  
<https://doi.org/10.1108/03321640710713930>
- El-Kady MA and Alshammari BM (2011). A practical framework for reliability and quality assessment of power systems. *Energy and Power Engineering*, 3(04): 499-507.  
<https://doi.org/10.4236/epe.2011.34060>
- El-Kady MA and Alshammari BM (2012). Assessment of reliability and quality levels in power systems. In the Asia-Pacific Power and Energy Engineering Conference, IEEE, Shanghai, China: 1-4.  
<https://doi.org/10.1109/APPEEC.2012.6307706>
- El-Kady MA, El-Sobki MS, and Sinha NK (1985). Loss of load probability evaluation based on real-time emergency dispatch. *Canadian Electrical Engineering Journal*, 10(2): 57-60.  
<https://doi.org/10.1109/CEEJ.1985.6592019>
- El-Kady MA, El-Sobki MS, and Sinha NK (1986). Reliability evaluation for optimally operated, large, electric power systems. *IEEE Transactions on Reliability*, 35(1): 41-47.  
<https://doi.org/10.1109/TR.1986.4335340>
- Goel L and Low LS (2001). Incorporating generator scheduling in composite power system well-being analysis. In the 2001 IEEE Porto Power Tech Proceedings, IEEE, Porto, Portugal.  
<https://doi.org/10.1109/PTC.2001.964879>
- Jirutitijaroen P and Singh C (2008). Reliability constrained multi-area adequacy planning using stochastic programming with sample-average approximations. *IEEE Transactions on Power Systems*, 23(2): 504-513.  
<https://doi.org/10.1109/TPWRS.2008.919422>
- Kolisnyk I, Oliynyk D, and Ponomarenko A (2019). On the reliability of electric power supply of electrical receiver in the electric networks. *Annals of Electrical and Electronic Engineering*, 2(4): 1-7.  
<https://doi.org/10.21833/AEEEE.2019.04.001>
- Pérez-Londoño SM, Olivar-Tost G, and Mora-Florez JJ (2017). Online determination of voltage stability weak areas for situational awareness improvement. *Electric Power Systems Research*, 145: 112-121.  
<https://doi.org/10.1016/j.epsr.2016.12.026>
- Teh J, Lai CM, and Cheng YH (2017). Impact of the real-time thermal loading on the bulk electric system reliability. *IEEE Transactions on Reliability*, 66(4): 1110-1119.  
<https://doi.org/10.1109/TR.2017.2740158>
- Wilson K and Wang J (2019). Optimized artificial neural network method for underground cables fault classification. *Annals of Electrical and Electronic Engineering*, 2(9): 18-24.  
<https://doi.org/10.21833/AEEEE.2019.09.004>
- Zhao JH, Dong ZY, Lindsay P, and Wong KP (2009). Flexible transmission expansion planning with uncertainties in an electricity market. *IEEE Transactions on Power Systems*, 24(1): 479-488.  
<https://doi.org/10.1109/TPWRS.2008.2008681>